## CONCEPTS FOR ADVANCED MATHEMATICS, C2 (4752) AS

## Objectives

To introduce students to a number of topics which are fundamental to the advanced study of mathematics.

## Assessment

Examination (72 marks)
1 hour 30 minutes.
The examination paper has two sections.
Section A: $\quad 8-10$ questions, each worth no more than 5 marks. Section Total: 36 marks

Section B: three questions, each worth about 12 marks.
Section Total: 36 marks

## Assumed Knowledge

Candidates are expected to know the content of Intermediate Tier GCSE and C1.

## Subject Criteria

The Units $C 1$ and $C 2$ are required for Advanced Subsidiary GCE Mathematics in order to ensure coverage of the subject criteria.

The Units $C 1, C 2, C 3$ and $C 4$ are required for Advanced GCE Mathematics in order to ensure coverage of the subject criteria.

## Calculators

In the MEI Structured Mathematics specification, no calculator is allowed in the examination for $C 1$. For all other units, including this one, a graphical calculator is allowed.

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## CONCEPTS FOR ADVANCED MATHEMATICS, C2

Specification $\quad$ Ref. $\quad$ Competence Statements

## ALGEBRA

Logarithms.
C2a1 Understand the meaning of the word logarithm.
2 Understand the laws of logarithms and how to apply them.

3 Know the values of $\log _{a} a$ and $\log _{a} 1$.
4 Know how to convert from an index to a logarithmic form and vice versa.
5 Know the function $y=a^{x}$ and its graph.
6 Be able to solve an equation of the form $a^{x}=b$.
7 Know how to reduce the equations $y=a x^{n}$ and $y=a b^{x}$ to linear form and, using experimental data, to draw a graph to find values of $a, n$ and $a, b$.

## SEQUENCES AND SERIES

| Definitions of $\quad$ C2s1 |
| :--- |
| sequences. | | Know what a sequence of numbers is and the meaning of finite and infinite |
| :--- |
| sequences. |

2 Know that a sequence can be generated using a formula for the $k^{\text {th }}$ term, or a recurrence relation of the form $a_{k+1}=\mathrm{f}\left(a_{k}\right)$.
3 Know what a series is.
4 Be familiar with $\sum$ notation.
5 Know and be able to recognise the periodicity of sequences.
6 Know the difference between convergent and divergent sequences.
Arithmetic series. 7 Know what is meant by arithmetic series and sequences.

8 Be able to use the standard formulae associated with arithmetic series and sequences.
Geometric series. 9 Know what is meant by geometric series and sequences.

10 Be able to use the standard formulae associated with geometric series and sequences.
11 Know the condition for a geometric series to be convergent and be able to find its sum to infinity.

12 Be able to solve problems involving arithmetic and geometric series and sequences.

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## TRIGONOMETRY

| Basic <br> trigonometry. | C2t1 | * Know how to solve right-angled triangles using trigonometry. |
| :--- | ---: | :--- |
| The sine, cosine <br> and tangent <br> functions. | 2 | Be able to use the definitions of $\sin \theta$ and $\cos \theta$ for any angle. |
|  | 3 | Know the graphs of $\sin \theta, \cos \theta$ and $\tan \theta$ for all values of $\theta$, their symmetries and <br> periodicities. |
| 4 | Know the values of $\sin \theta, \cos \theta$ and $\tan \theta$ when $\theta$ is $0^{\circ}, 30^{\circ}, 45^{\circ}, 60^{\circ}, 90^{\circ}$ and <br> $180^{\circ}$. |  |
| Identities. | 5 | Be able to use $\tan \theta=\frac{\sin \theta}{\cos \theta}$ (for any angle). |
| 6 | Be able to use the identity $\sin ^{2} \theta+\cos ^{2} \theta=1$. |  |
| 7 | Be able to solve simple trigonometric equations in given intervals. |  |


| Area of a triangle. | 8 | Know and be able to use the fact that the area of a triangle is given by $1 / 2 a b \sin C$. |
| :--- | :---: | :--- |
| The sine and <br> cosine rules. | 9 | Know and be able to use the sine and cosine rules. |
| Radians. | 10 | Understand the definition of a radian and be able to convert between radians and <br> degrees. |
| 11 | Know and be able to find the arc length and area of a sector of a circle, when the <br> angle is given in radians. |  |

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## CALCULUS

The basic process of differentiation.

C2c1 Know that the gradient of a curve at a point is given by the gradient of the tangent at the point.
2 Know that the gradient of the tangent is given by the limit of the gradient of a chord.

3
Know that the gradient function $\frac{\mathrm{d} y}{\mathrm{~d} x}$ gives the gradient of the curve and measures the rate of change of $y$ with respect to $x$.

Applications of differentiation to the graphs of functions.

4 Be able to differentiate $y=k x^{n}$ where $k$ is a constant, and the sum of such functions.
5 Be able to find second derivatives.

6 Be able to use differentiation to find stationary points on a curve: maxima, minima and points of inflection.
7 Understand the terms increasing function and decreasing function.

8 Be able to find the equation of a tangent and normal at any point on a curve.

Integration as the inverse of differentiation.

9 Know that integration is the inverse of differentiation.
10 Be able to integrate functions of the form $k x^{n}$ where $k$ is a constant and $n \neq-1$, and the sum of such functions.
11 Know what are meant by indefinite and definite integrals.
12 Be able to evaluate definite integrals.

13 Be able to find a constant of integration given relevant information.

Integration to find the area under a curve.

14 Know that the area under a graph can be found as the limit of a sum of areas of rectangles.

15 Be able to use integration to find the area between a graph and the $x$-axis.

16 Be able to find an approximate value of a definite integral using the trapezium rule, and comment sensibly on its accuracy.

## CURVE SKETCHING

Stationary points. $\mathrm{C} 2 \mathrm{C} 1 \quad \mathrm{Be}$ able to use stationary points when curve sketching.

Stretches.
2 Know how to sketch curves of the form $y=a \mathrm{f}(x)$ and $y=\mathrm{f}(a x)$, given the curve of: $y=\mathrm{f}(x)$.

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