CONCEPTS FOR ADVANCED MATHEMATICS, C2 (4752) AS

Objectives

To introduce students to a number of topics which are fundamental to the advanced study of mathematics.

Assessment

Examination	(72 marks)1 hour 30 minutes.The examination paper has two sections.		
	Section A:	8-10 questions, each worth no more than 5 marks. Section Total: 36 marks	
	Section B:	three questions, each worth about 12 marks. Section Total: 36 marks	

Assumed Knowledge

Candidates are expected to know the content of Intermediate Tier GCSE and C1.

Subject Criteria

The Units *C1* and *C2* are required for Advanced Subsidiary GCE Mathematics in order to ensure coverage of the subject criteria.

The Units *C1*, *C2*, *C3* and *C4* are required for Advanced GCE Mathematics in order to ensure coverage of the subject criteria.

Calculators

In the MEI Structured Mathematics specification, no calculator is allowed in the examination for *C1*. For all other units, including this one, a graphical calculator is allowed.

CONCEPTS FOR ADVANCED MATHEMATICS, C2		
Specification	Ref.	Competence Statements
		ALGEBRA
Logarithms.	C2a1	Understand the meaning of the word logarithm.
	2	Understand the laws of logarithms and how to apply them.
	3	Know the values of $\log_a a$ and $\log_a 1$.
	4	Know how to convert from an index to a logarithmic form and vice versa.
	5	Know the function $y = a^x$ and its graph.
	6	Be able to solve an equation of the form $a^x = b$.
	7	Know how to reduce the equations $y = ax^n$ and $y = ab^x$ to linear form and,
		using experimental data, to draw a graph to find values of a, n and a, b .

		SEQUENCES AND SERIES
Definitions of sequences.	C2s1	Know what a sequence of numbers is and the meaning of finite and infinite sequences.
-	2	Know that a sequence can be generated using a formula for the k^{th} term, or a recurrence relation of the form $a_{k+1} = f(a_k)$.
-	3	Know what a series is.
-	4	Be familiar with \sum notation.
	5	Know and be able to recognise the periodicity of sequences.
	6	Know the difference between convergent and divergent sequences.
Arithmetic series.	7	Know what is meant by arithmetic series and sequences.
	8	Be able to use the standard formulae associated with arithmetic series and sequences.
Geometric series.	9	Know what is meant by geometric series and sequences.
-	10	Be able to use the standard formulae associated with geometric series and sequences.
	11	Know the condition for a geometric series to be convergent and be able to find its sum to infinity.
	12	Be able to solve problems involving arithmetic and geometric series and sequences.

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	TRIGONOMETRY		
Basic trigonometry.	C2t1	* Know how to solve right-angled triangles using trigonometry.	
The sine, cosine	2	Be able to use the definitions of $\sin \theta$ and $\cos \theta$ for any angle.	
and tangent functions.	3	Know the graphs of sin θ , cos θ and tan θ for all values of θ , their symmetries and periodicities.	
-	4	Know the values of $\sin \theta$, $\cos \theta$ and $\tan \theta$ when θ is 0°, 30°, 45°, 60°, 90° and 180°.	
Identities.	5	Be able to use $\tan \theta = \frac{\sin \theta}{\cos \theta}$ (for any angle).	
	6	Be able to use the identity $\sin^2 \theta + \cos^2 \theta = 1$.	
	7	Be able to solve simple trigonometric equations in given intervals.	
Area of a triangle.	8	Know and be able to use the fact that the area of a triangle is given by $\frac{1}{2}ab\sin C$.	
The sine and cosine rules.	9	Know and be able to use the sine and cosine rules.	
Radians.	10	Understand the definition of a radian and be able to convert between radians and degrees.	
-	11	Know and be able to find the arc length and area of a sector of a circle, when the angle is given in radians.	

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		CALCULUS
The basic process of differentiation.	C2c1	Know that the gradient of a curve at a point is given by the gradient of the tangen at the point.
	2	Know that the gradient of the tangent is given by the limit of the gradient of a chord.
-	3	Know that the gradient function $\frac{dy}{dx}$ gives the gradient of the curve and measures
		the rate of change of <i>y</i> with respect to <i>x</i> .
Applications of differentiation to the graphs of	4	Be able to differentiate $y = kx^n$ where <i>k</i> is a constant, and the sum of such functions.
functions.	5	Be able to find second derivatives.
	6	Be able to use differentiation to find stationary points on a curve: maxima, minima and points of inflection.
	7	Understand the terms increasing function and decreasing function.
	8	Be able to find the equation of a tangent and normal at any point on a curve.
Integration as the	9	Know that integration is the inverse of differentiation.
inverse of differentiation.	10	Be able to integrate functions of the form kx^n where k is a constant and $n \neq -1$, and the sum of such functions.
	11	Know what are meant by indefinite and definite integrals.
-	12	Be able to evaluate definite integrals.
	13	Be able to find a constant of integration given relevant information.
Integration to find the area under a curve.	14	Know that the area under a graph can be found as the limit of a sum of areas of rectangles.
	15	Be able to use integration to find the area between a graph and the <i>x</i> -axis.
	16	Be able to find an approximate value of a definite integral using the trapezium rule, and comment sensibly on its accuracy.

CURVE SKETCHING		
Stationary points.	C2C1	Be able to use stationary points when curve sketching.
Stretches.	2	Know how to sketch curves of the form $y = af(x)$ and $y = f(ax)$, given the curve of: $y = f(x)$.