

**ADVANCED SUBSIDIARY GCE
MATHEMATICS (MEI)**

Statistics 1

4766

QUESTION PAPER

Candidates answer on the printed answer book.

OCR supplied materials:

- Printed answer book 4766
- MEI Examination Formulae and Tables (MF2)

Other materials required:

- Scientific or graphical calculator

**Thursday 26 May 2011
Morning**

Duration: 1 hour 30 minutes

INSTRUCTIONS TO CANDIDATES

These instructions are the same on the printed answer book and the question paper.

- The question paper will be found in the centre of the printed answer book.
- Write your name, centre number and candidate number in the spaces provided on the printed answer book. Please write clearly and in capital letters.
- **Write your answer to each question in the space provided in the printed answer book.** Additional paper may be used if necessary but you must clearly show your candidate number, centre number and question number(s).
- Use black ink. Pencil may be used for graphs and diagrams only.
- Read each question carefully. Make sure you know what you have to do before starting your answer.
- Answer **all** the questions.
- Do **not** write in the bar codes.
- You are permitted to use a scientific or graphical calculator in this paper.
- Final answers should be given to a degree of accuracy appropriate to the context.

INFORMATION FOR CANDIDATES

This information is the same on the printed answer book and the question paper.

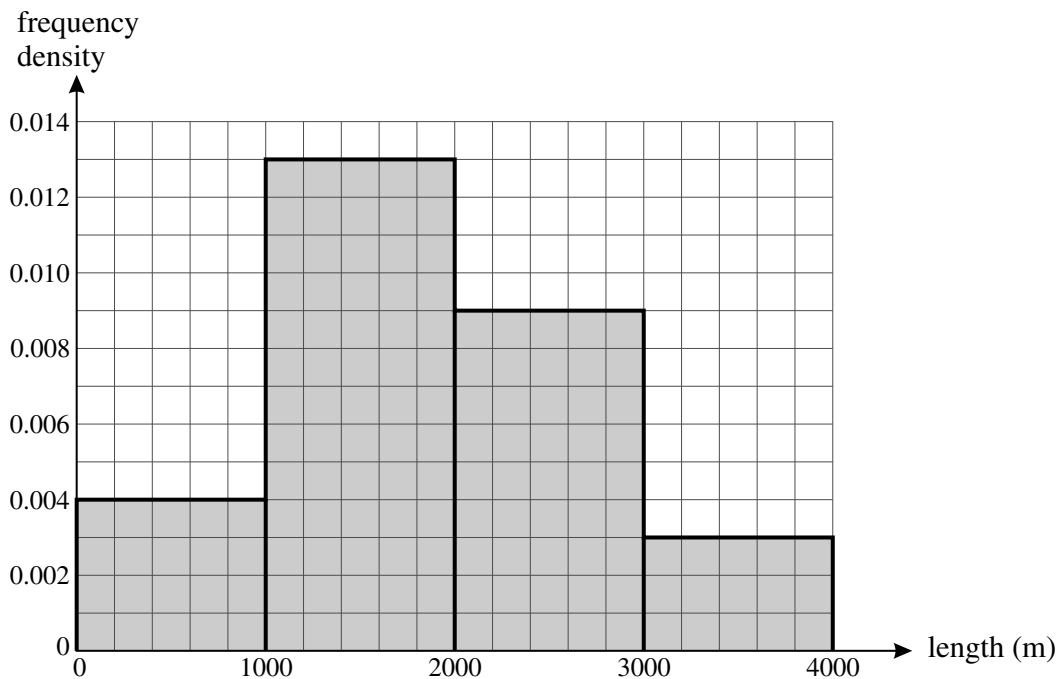
- The number of marks is given in brackets [] at the end of each question or part question on the question paper.
- You are advised that an answer may receive **no marks** unless you show sufficient detail of the working to indicate that a correct method is being used.
- The total number of marks for this paper is **72**.
- The printed answer book consists of **12** pages. The question paper consists of **4** pages. Any blank pages are indicated.

INSTRUCTION TO EXAMS OFFICER / INVIGILATOR

- Do not send this question paper for marking; it should be retained in the centre or destroyed.

Section A (36 marks)

- 1 In the Paris-Roubaix cycling race, there are a number of sections of cobbled road. The lengths of these sections, measured in metres, are illustrated in the histogram.



- (i) Find the number of sections which are between 1000 and 2000 metres in length. [2]
- (ii) Name the type of skewness suggested by the histogram. [1]
- (iii) State the minimum and maximum possible values of the midrange. [2]
- 2 I have 5 books, each by a different author. The authors are Austen, Brontë, Clarke, Dickens and Eliot.
- (i) If I arrange the books in a random order on my bookshelf, find the probability that the authors are in alphabetical order with Austen on the left. [2]
- (ii) If I choose two of the books at random, find the probability that I choose the books written by Austen and Brontë. [3]
- 3 25% of the plants of a particular species have red flowers. A random sample of 6 plants is selected.
- (i) Find the probability that there are no plants with red flowers in the sample. [2]
- (ii) If 50 random samples of 6 plants are selected, find the expected number of samples in which there are no plants with red flowers. [2]

- 4 Two fair six-sided dice are thrown. The random variable X denotes the difference between the scores on the two dice. The table shows the probability distribution of X .

r	0	1	2	3	4	5
$P(X = r)$	$\frac{1}{6}$	$\frac{5}{18}$	$\frac{2}{9}$	$\frac{1}{6}$	$\frac{1}{9}$	$\frac{1}{18}$

(i) Draw a vertical line chart to illustrate the probability distribution. [2]

(ii) Use a probability argument to show that

(A) $P(X = 1) = \frac{5}{18}$, [2]

(B) $P(X = 0) = \frac{1}{6}$. [1]

(iii) Find the mean value of X . [2]

- 5 In a recent survey, a large number of working people were asked whether they worked full-time or part-time, with part-time being defined as less than 25 hours per week. One of the respondents is selected at random.

- W is the event that this person works part-time.
- F is the event that this person is female.

You are given that $P(W) = 0.14$, $P(F) = 0.41$ and $P(W \cap F) = 0.11$.

(i) Draw a Venn diagram showing the events W and F , and fill in the probability corresponding to each of the four regions of your diagram. [3]

(ii) Determine whether the events W and F are independent. [2]

(iii) Find $P(W | F)$ and explain what this probability represents. [3]

- 6 The numbers of eggs laid by a sample of 70 female herring gulls are shown in the table.

Number of eggs	1	2	3	4
Frequency	10	40	15	5

(i) Find the mean and standard deviation of the number of eggs laid per gull. [5]

(ii) The sample did not include female herring gulls that laid no eggs. How would the mean and standard deviation change if these gulls were included? [2]

Section B (36 marks)

- 7 Any patient who fails to turn up for an outpatient appointment at a hospital is described as a 'no-show'. At a particular hospital, on average 15% of patients are no-shows. A random sample of 20 patients who have outpatient appointments is selected.

(i) Find the probability that

(A) there is exactly 1 no-show in the sample, [3]

(B) there are at least 2 no-shows in the sample. [2]

The hospital management introduces a policy of telephoning patients before appointments. It is hoped that this will reduce the proportion of no-shows. In order to check this, a random sample of n patients is selected. The number of no-shows in the sample is recorded and a hypothesis test is carried out at the 5% level.

(ii) Write down suitable null and alternative hypotheses for the test. Give a reason for your choice of alternative hypothesis. [4]

(iii) In the case that $n = 20$ and the number of no-shows in the sample is 1, carry out the test. [4]

(iv) In another case, where n is large, the number of no-shows in the sample is 6 and the critical value for the test is 8. Complete the test. [3]

(v) In the case that $n \leq 18$, explain why there is no point in carrying out the test at the 5% level. [2]

- 8 The heating quality of the coal in a sample of 50 sacks is measured in suitable units. The data are summarised below.

Heating quality (x)	$9.1 \leq x \leq 9.3$	$9.3 < x \leq 9.5$	$9.5 < x \leq 9.7$	$9.7 < x \leq 9.9$	$9.9 < x \leq 10.1$
Frequency	5	7	15	16	7

(i) Draw a cumulative frequency diagram to illustrate these data. [5]

(ii) Use the diagram to estimate the median and interquartile range of the data. [3]

(iii) Show that there are no outliers in the sample. [3]

(iv) Three of these 50 sacks are selected at random. Find the probability that

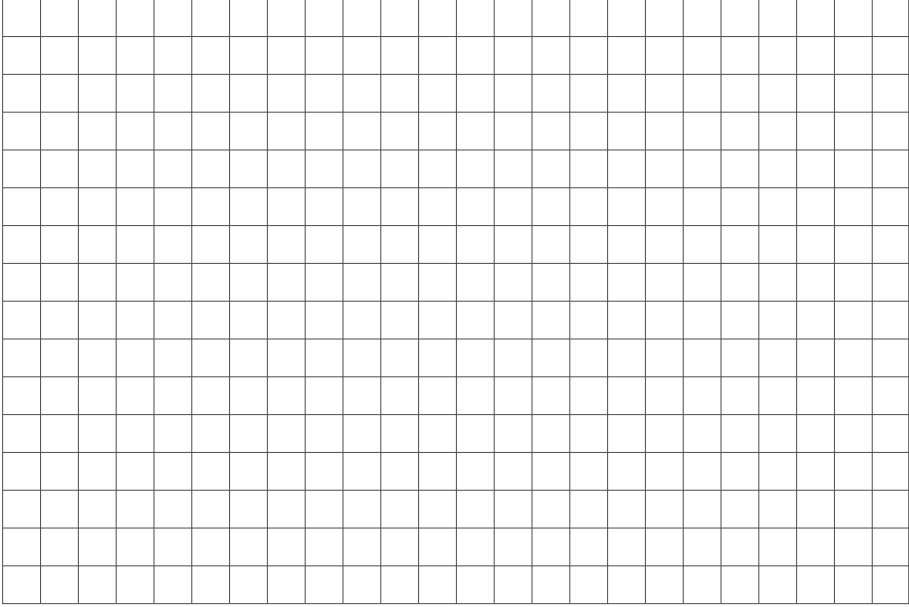
(A) in all three, the heating quality x is more than 9.5, [3]

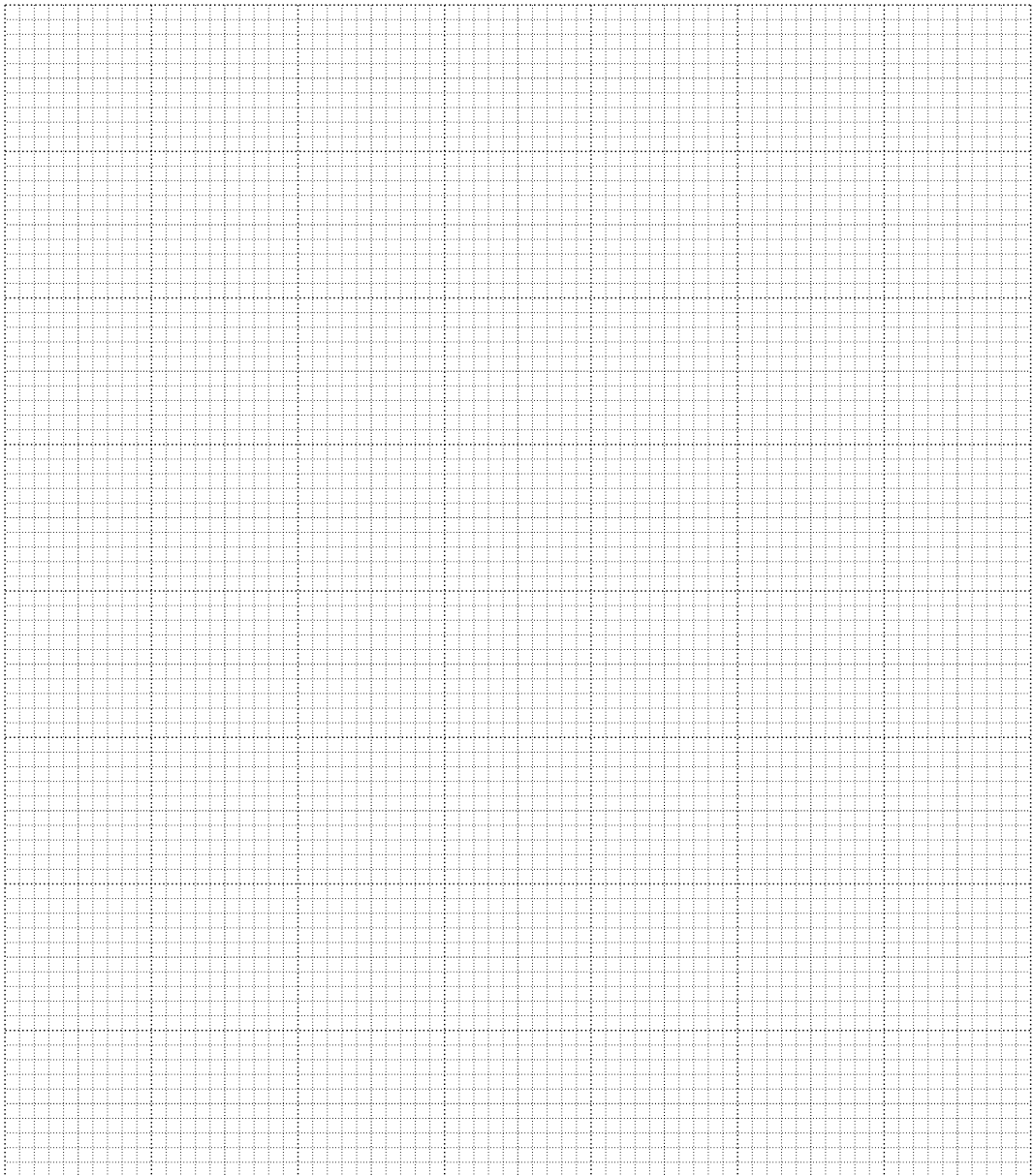
(B) in at least two, the heating quality x is more than 9.5. [4]

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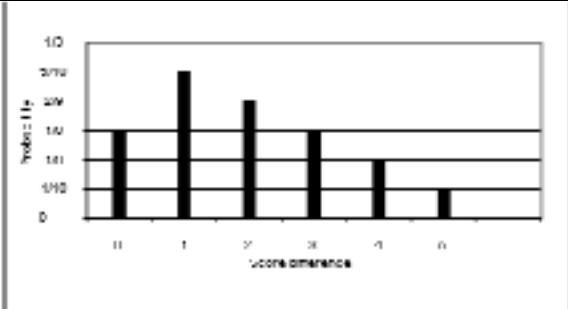
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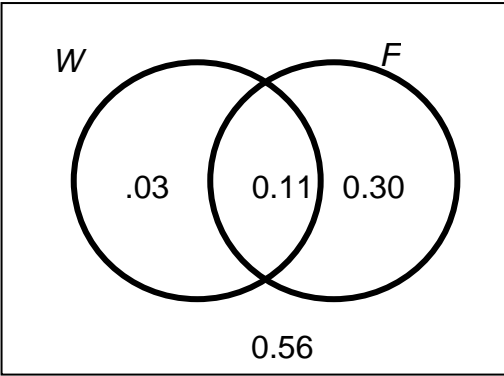
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8 (i)

	SECTION A			
Q1 (i)	$1000 \times 0.013 = 13$ Or $0.2 \times 65 = 13$ Or $0.2 \times 5 \times 13 = 13$	M1 A1 M1 for 0.2×65	2	Allow with or without working For MR $1000 \times 0.13 = 130$ Allow M1A0 Allow M1A0 if extra terms added eg 1000×0.004 SC1 for $1000 \times 0.014 = 14$ For whole calculation
(ii)	Positive	B1	1	Allow +ve but NOT skewed to the right Do not allow 'positive correlation'
(iii)	Minimum value = 1500 Maximum value = 2500	B1 Without wrong working B1 Without wrong working	2	Exact answers only unless good explanation such as eg no road has length zero so min is eg 1501 SC1 for lower answer between 1499 and 1501 and upper between 2499 and 2501 Allow answer given as inequality
		TOTAL	5	
Q2 (i)	Either $P(\text{alphabetic order}) = \frac{1}{5} \times \frac{1}{4} \times \frac{1}{3} \times \frac{1}{2} \times \frac{1}{1} = \frac{1}{120}$ or $P(\text{alphabetic order}) = \frac{1}{5!} = \frac{1}{120} = 0.00833$	M1 for 5! or 120 or 5P_5 seen or product of correct fractions A1 CAO	2	Allow 0.0083 or 1/120 but not 0.008
(ii)	Either $P(\text{picks Austen and Bronte}) = \frac{2}{5} \times \frac{1}{4} = \frac{1}{10}$ or $P(\text{picks Austen and Bronte}) = \frac{1}{5} \times \frac{1}{4} \times 2 = \frac{1}{10}$ or $P(\text{picks Austen and Bronte}) = \frac{1}{\binom{5}{2}} = \frac{1}{10}$	M1 for denominators M1 for $2 \times$ <i>dep on correct denominators</i> A1 CAO Or M1 for $\binom{5}{2}$ or 10 M1 for $1/\binom{5}{2}$ A1 CAO	3	$1/5P_2$ scores M1 also 1/20 oe scores M1 even if followed by further incorrect working $\binom{5}{2}$ seen as part of a binomial expression gets M0M0A0
		TOTAL	5	

Q3 (i)	$P(X=0) = 0.75^6 = 0.178$	M1 for 0.75^6 A1 CAO	2	Or from tables 0.1780 Or 729/4096 Allow 0.18 with working
(ii)	$E(X) = np = 50 \times 0.178 = 8.9$	M1 for product A1 FT	2	FT their answer to (i) providing it's a probability NB A0 if subsequently rounded
		TOTAL	4	
Q4 (i)		G1 labelled linear scales on both axes G1 heights	2	Accept r or x for horizontal label and p or better for vertical including probability distribution Visual check only Allow G1G0 for points rather than lines Bars must not be wider than gaps for second G1 Condone vertical scale 1, 2, 3, 4, 5 and Probability (\times) 1/18 as label BOD for height of $r = 0$ on vertical axis
(ii)	<p>(A) If $X = 1$, possible scores are (1,2), (2,3), (3,4), (4,5), (5,6) and (2,1), (3,2), (4,3), (5,4), (6,5)</p> <p>(All are equally likely) so probability = $\frac{10}{36} = \frac{5}{18}$</p> <p>(B) If $X = 0$, possible scores are (1,1), (2,2), (3,3), (4,4), (5,5), (6,6) so probability = $\frac{6}{36} = \frac{1}{6}$</p>	M1 A1 B1	2 1	<p>Also M1 for a clear correct sample space seen with the ten 1's identified by means of circles or ticks oe soi. Must be convincing. No additional values such as 0,1 and 1,0 Do not allow 'just 10 ways you can have a difference of 1 so 10/36' or equivalent SC1 for possible scores are (1,2), (2,3), (3,4), (4,5), (5,6) so probability = $2 \times 5 \times 1/36$ with no explanation for $2 \times$</p> <p>Also B1 for a clear correct sample space seen with the six 0's identified by means of circles or ticks oe soi. Must be convincing. No additional values. Allow both dice must be the same so probability = $6/36 = 1/6$. Allow $1 \times 1/6 = 1/6$ BOD</p>
(iii)	<p>Mean value of $X =$</p> $0 \times \frac{1}{6} + 1 \times \frac{5}{18} + 2 \times \frac{2}{9} + 3 \times \frac{1}{6} + 4 \times \frac{1}{9} + 5 \times \frac{1}{18} = 1\frac{17}{18} = 1.94$	M1 for $\sum rp$ (at least 3 terms correct) A1 CAO	2	Or 35/18 Division by 6 or other spurious factor gets MAX M1A0
		TOTAL	7	

Q5 (i)		<p>G1 for two labelled intersecting circles</p> <p>G1 for at least 2 correct probabilities.</p> <p>G1 for remaining correct probabilities</p>	<p>3</p>	<p>Allow labels such as P(W) and P(F)</p> <p>Allow other sensible shapes in place of circles</p>
(ii)	$P(W) \times P(F) = 0.14 \times 0.41 = 0.0574 \neq P(W \cap F) = 0.11$ So not independent.	<p>M1 for 0.41×0.14</p> <p>A1 Condone dependent</p> <p>Must have full method</p> <p>www</p> <p>Must have either $P(W \cap F)$ or 0.11</p>	<p>2</p>	<p>Answer of 0.574 gets Max M1A0</p> <p>Omission of 0.0574 gets M1A0 Max</p> <p>Or:</p> <p>$P(W F) = 0.11/0.41 = 0.268 \neq P(W) (= 0.14)$ M1 for full working</p> <p>$P(F W) = 0.11/0.14 = 0.786 \neq P(F) (= 0.41)$ M1 for full working</p> <p>No marks without correct working</p>
(iii)	$P(W F) = \frac{P(W \cap F)}{P(F)} = \frac{0.11}{0.41} = \frac{11}{41} = 0.268$ <p>This is the probability that a randomly selected respondent works (part time), given that the respondent is female.</p>	<p>M1 for correct fraction</p> <p>A1</p> <p>E1</p> <p>For E1 must be in context – not just talking about events F and W</p>	<p>3</p>	<p>Allow 0.27 with working</p> <p>Allow 11/41 as final answer</p> <p>Condone ‘if’ or ‘when’ for ‘given that’ but not the words ‘and’ or ‘because’ or ‘due to’ for E1.</p> <p>E1 (independent of M1): the order/structure must be correct i.e. no reverse statement</p> <p>Allow ‘The probability that a randomly selected female respondent works part time’ oe</p>
		<p>TOTAL</p>	<p>8</p>	

Q6 (i)	$\text{Mean} = \frac{1 \times 10 + 2 \times 40 + 3 \times 15 + 4 \times 5}{70} = \frac{155}{70} = 2.214$ $S_{xx} =$ $1^2 \times 10 + 2^2 \times 40 + 3^2 \times 15 + 4^2 \times 5 - \frac{155^2}{70} = 385 - 343.21 = 41.79$ $s = \sqrt{\frac{41.79}{69}} = 0.778$	<p>M1 A1 CAO</p> <p>M1 for Σfx^2 s.o.i.</p> <p>M1 for attempt at S_{xx} Dep on first M1</p> <p>A1 CAO If 0.778 or better seen ignore previous incorrect working (calculator answer) Allow final answer to 2 sig fig (www)</p>	<p>5</p>	<p>For M1 allow sight of at least 3 double pairs seen from $1 \times 10 + 2 \times 40 + 3 \times 15 + 4 \times 5$ with divisor 70. Allow answer of 155/70 or 2.2 or 2.21 or 31/14 oe For 155/70 = eg 2.3 , allow A1 isw</p> <p>M1 for $1^2 \times 10 + 2^2 \times 40 + 3^2 \times 15 + 4^2 \times 5$ with at least three correct terms Using exact mean leads to $S_{xx} = 41.79$, $s=0.778$, Using mean 2.214 leads to $S_{xx} = 41.87$, $s=0.779$, Using mean 2.21 leads to $S_{xx} = 43.11$ and $s = 0.790$ Using mean 2.2 leads to $S_{xx} = 46.2$ and $s = 0.818$ Using mean 2 leads to $S_{xx} = 105$ and $s = 1.233$ All the above get M1M1A1 except the last one which gets M1M1A0 RMSD(divisor n rather than $n - 1$) = $\sqrt{(41.79/70)} = 0.772$ gets M1M1A0 Alternative method, award M1 for at least 3 terms of and second M1 for all 4 terms of $(1 - 2.214)^2 \times 10 + (2 - 2.214)^2 \times 40 + (3 - 2.214)^2 \times 15 + (4 - 2.214)^2 \times 5 (= 41.79)$ NB Allow full credit for correct answers without working (calculator used)</p>
(ii)	<p>Mean would decrease</p> <p>Standard deviation would increase</p>	<p>B1</p> <p>B1</p>	<p>2</p>	<p>Do not accept increase/decrease seen on their own – must be linked to mean and SD. Allow eg ‘It would skew the mean towards zero’ And eg ‘ It would stretch the SD’ SC1 for justified argument that standard deviation might either increase or decrease according to number with no eggs ($n \leq 496$ increase, $n \geq 497$ decrease)</p>
		TOTAL	7	

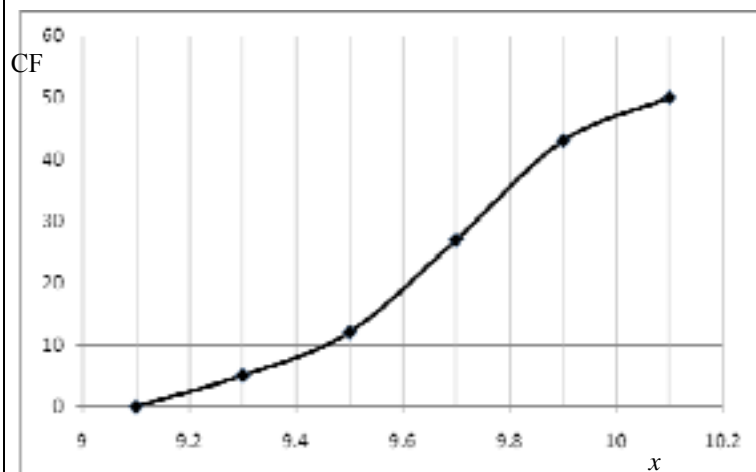
	SECTION B			
Q7 (i)	$X \sim B(20, 0.15)$ (A) Either $P(X = 1) = \binom{20}{1} \times 0.15^1 \times 0.85^{19} = 0.1368$ or $P(X = 1) = P(X \leq 1) - P(X \leq 0)$ $= 0.1756 - 0.0388 = 0.1368$ (B) $P(X \geq 2) = 1 - P(X \leq 1)$ $= 1 - 0.1756 = 0.8244$	M1 $0.15^1 \times 0.85^{19}$ M1 $\binom{20}{1} \times p^1 q^{19}$ A1 CAO OR: M2 for $0.1756 - 0.0388$ A1 CAO M1 for $1 - \text{their } 0.1756$ A1 CAO		<p>3</p> <p>With $p + q = 1$ Allow answer 0.137 with or without working or 0.14 if correct working shown See tables at the website http://www.mei.org.uk/files/pdf/formula_book_mf2.pdf For misread of tables $0.3917 - 0.1216 = 0.2701$ allow M1M1A0 also for $0.1304 - 0.0261 = 0.1043$</p> <p>2</p> <p>Provided 0.1756 comes from $P(X=0) + P(X=1)$ Allow answer 0.824 with or without working or 0.82 if correct working shown</p> <p>Point probability method: $P(1) = 0.1368$, $P(0) = 0.0388$ So $1 - P(X \leq 1) = 1 - 0.1756$ gets M1 then mark as per scheme M0A0 for $1 - P(X \leq 1) = 1 - 0.4049 = 0.5951$</p> <p>For misread of tables $1 - 0.3917 = 0.6083$ allow M1A1 also for $1 - 0.1304 = 0.8696$ provided consistent with part (A) OR M1A0 if formula used in part (A)</p>

(ii)	<p>Let $X \sim B(n, p)$ Let p = probability of a 'no-show' (for population) $H_0: p = 0.15$ $H_1: p < 0.15$</p> <p>H_1 has this form because the hospital management hopes to reduce the proportion of no-shows.</p>	<p>B1 for definition of p B1 for H_0 B1 for H_1</p> <p>E1 Allow correct answer even if H_1 wrong</p>	<p>4</p> <p>Allow $p = P(\text{no-show})$ for B1 Definition of p must include word probability (or chance or proportion or percentage or likelihood but NOT possibility). Preferably as a separate comment. However can be at end of H_0 as long as it is a clear definition 'p = the probability of no-show, NOT just a sentence 'probability is 0.15' $H_0: p(\text{no-show}) = 0.15$, $H_1: p(\text{no-show}) < 0.15$ gets B0B1B1 Allow $p=15\%$, allow θ or π and ρ but not x. However allow any single symbol <u>if defined</u> Allow $H_0 = p=0.15$, Do not allow $H_0: P(X=x) = 0.15$, $H_1: P(X=x) < 0.15$ Do not allow $H_0: =0.15$, $=15\%$, $P(0.15)$, $p(0.15)$, $p(x)=0.15$, $x=0.15$ (unless x correctly defined as a probability) Do not allow $H_1: p \leq 0.15$, Do not allow H_0 and H_1 reversed for B marks but can still get E1 Allow NH and AH in place of H_0 and H_1 For hypotheses given in words allow Maximum B0B1B1E1 Hypotheses in words must include probability (or chance or proportion or percentage) and the figure 0.15 oe.</p>
(iii)	<p>$P(X \leq 1) = 0.1756 > 5\%$</p> <p>So not enough evidence to reject H_0. Not significant. Conclude that there is not enough evidence to indicate that the proportion of no-shows has decreased.</p>	<p>M1 for probability seen, but not in calculation for point probability M1 dep for comparison A1</p>	<p>4</p> <p>Zero for use of point prob - $P(X = 1) = 0.1368$ Do <u>NOT</u> FT wrong H_1 Allow accept H_0, or reject H_1 Full marks only available if 'not enough evidence to...' oe mentioned somewhere Do not allow 'enough evidence to reject H_1' for final mark but can still get 3/4 Upper end comparison: $1 - 0.1756 = 0.8244 < 95\%$ gets</p>

	Note: use of critical region method scores M1 for region $\{0\}$ M1 for 1 does not lie in critical region, then A1 E1 as per scheme	E1 dep for conclusion in context.		M2 then A1E1 as per scheme <u>Line diagram method</u> M1 for squiggly line between 0 and 1 with arrow pointing to left, M1 0.0388 seen on diagram from squiggly line or from 0, A1E1 for correct conclusion <u>Bar chart method</u> M1 for line clearly on boundary between 0 and 1 and arrow pointing to left, M1 0.0388 seen on diagram from boundary line or from 0, A1E1 for correct conclusion
(iv)	$6 < 8$ So there is sufficient evidence to reject H_0 Conclude that there is enough evidence to indicate that the proportion of no-shows appears to have decreased.	M1 for comparison seen A1 E1 for conclusion in context	3	Allow '6 lies in the CR' Do NOT insist on 'not enough evidence' here Do not FT wrong $H_1: p > 0.15$ but may get M1 In part (iv) ignore any interchanged H_0 and H_1 seen in part (ii)
(v)	For $n \leq 18$, $P(X \leq 0) > 0.05$ so the critical region is empty.	E1 for $P(X \leq 0) > 0.05$ E1 indep for critical region is empty	2	E1 also for sight of 0.0536 Condone $P(X = 0) > 0.05$ or all probabilities or values, (but not outcomes) in table (for $n \leq 18$) > 0.05 Or 'There is no critical region' For second E1 accept ' H_0 would always be accepted' Do NOT FT wrong H_1 Use professional judgement - allow other convincing answers
		TOTAL	18	

Q8
(i)

Upper Bound	9.1	9.3	9.5	9.7	9.9	10.1
Cumulative frequency	0	5	12	27	43	50



B1 for cumulative frequencies

G1 for scales

G1 for labels

G1 for points
(Provided plotted at correct UCB positions)

G1 for joining points

All G's dep on attempt at cumulative frequency but not cumulative fx's or other spurious values.

May be implied from graph. Condone omission of 0 at this stage.

Linear horizontal scale.

Linear vertical scale: 0 to 50

(no inequality scales - Not even <9.1 , <9.3 , <9.5 ...)Heating quality or x and Cumulative frequency or just CF or similar but not just frequency or fd nor cumulative fd**5** Plotted as (UCB, their cf). Ignore (9.1,0) at this stage. No midpoint or LCB plots.
Plotted within $\frac{1}{2}$ small squareFor joining all of 'their points' (line or smooth curve)
AND now including (9.1,0) dep on previous G1

Mid point or LCB plots may score first three marks

Can get up to 3/5 for cum freq bars
Allow full credit if axes reversed correctly

Lines of best fit could attract max 4 out of 5.

(ii)

Median = 9.67

B1 FT
Allow answers between 9.66 and 9.68 without checking curve.
Otherwise check curve.**3**Based on 25th to 26th value on a cumulative frequency graph
ft their mid-point plot (not LCB's) approx 9.57 for m.p.
plot Allow 9.56 to 9.58 without checking
B0 for interpolation

	$Q1 = 9.51 \quad Q3 = 9.83$ Inter-quartile range = $9.83 - 9.51 = 0.32$	B1 FT for Q3 or Q1 B1 FT for IQR providing both Q1 and Q3 are correct Allow answers between 9.50 and 9.52 and between 9.82 and 9.84 without checking curve. Otherwise check curve.		Based on 12 th to 13 th and 37 th to 38 th values on a cumulative frequency graph ft their mid -point plot (not LCB's) approx $Q1 = 9.42$; $Q3 = 9.73$ Allow 9.41 to 9.43 and 9.72 to 9.74 without checking B0 for interpolation Allow correct IQR from graph if quartiles not stated Lines of best fit: B0 B0 B0 here.
(iii)	Lower limit $9.51 - 1.5 \times 0.32 = 9.03$ Upper limit $9.83 + 1.5 \times 0.32 = 10.31$ Thus there are no outliers in the sample.	B1 FT their Q_1 , IQR B1 FT their Q_3 , IQR E1 NB E mark dep on both B marks	3	Any use of <u>median</u> ± 1.5 IQR scores B0 B0 E0 If FT leads to limits above 9.1 or below 10.1 then E0 No marks for ± 2 or 3 IQR In this part FT their values from (ii) if sensibly obtained (eg from LCB plot) or lines of best fit, but not from location ie 12.5, 37.5 or cumulative fx's or similar. For use of mean $\pm 2s$, Mean = 9.652, $s = 0.235$, Limits 9.182, 10.122 gets M1 for correct lower limit, M1 for correct upper limit, zero otherwise, but E0 since there could be outliers using this definition
(iv)	(A) $P(\text{All 3 more than 9.5}) = \frac{38}{50} \times \frac{37}{49} \times \frac{36}{48} = 0.4304$ (=50616/117600 = 2109/4900)	M1 for $38/50 \times$ (triple product) M1 for product of remaining fractions A1 CAO	3	$(38/50)^3$ which gives answer 0.4389 scores M1M0A0 so watch for this. M0M0A0 for binomial probability including 0.76^{100} but ${}^3C_0 \times 0.24^0 \times 0.76^3$ still scores M1 $(k/50)^3$ for values of k other than 38 scores M0M0A0 $\frac{k}{50} \times \frac{(k-1)}{49} \times \frac{(k-2)}{48}$ for values of k other than 38 scores M1M0A0 Correct working but then multiplied or divided by some factor scores M1M0A0

	<p>(B) $P(\text{At least 2 more than 9.5}) = 3 \times \frac{38}{50} \times \frac{37}{49} \times \frac{12}{48} + 0.4304$ $= 3 \times 0.1435 + 0.4304$ $= 0.4304 + 0.4304$ $= 0.861$ $(=101232/117600 = 4218/4900 = 2109/2450)$</p> <p>OR</p> <p>$P(\text{At least 2 more than 9.5}) = 1 - (P(0) + P(1))$ $= 1 - \left[\left(\frac{12}{50} \times \frac{11}{49} \times \frac{10}{48} \right) + \left(3 \times \frac{12}{50} \times \frac{11}{49} \times \frac{38}{48} \right) \right]$ $= 1 - [0.01122 + 0.12796] = 1 - 0.13918 = 0.861$</p>	<p>M1 for product of 3 correct fractions seen M1 for $3 \times$ a sensible triple or sum of 3 sensible triples M1 indep for $+ 0.4304$ FT (providing it is a probability) A1 CAO</p> <p>M1 for $12/50 \times 11/49 \times 38/48$ M1 for $3 \times$ a sensible triple or sum of 3 sensible triples M1 dep on both previous M1's for $1 - [0.01122 + 0.12796]$ A1 CAO</p>	<p>4</p>	<p>Accept 0.43 with working and 0.430 without working Or $\binom{38}{3} / \binom{50}{3} = 2109/4900 = 0.4304$</p> <p>Allow unsimplified fraction as final answer 50616/117600</p> <p>Or $\binom{38}{2} \binom{12}{1} / \binom{50}{3} = 0.4304$ gets first two M1M1's</p> <p>SC1 for $3 \times \frac{38}{50} \times \frac{38}{50} \times \frac{12}{50}$ or other sensible triple and SC2 if this $+ \text{their } 0.4304 (= 0.8549)$ Allow 0.86 or 2109/2450 or 4218/4900, but only M3A0 for other unsimplified fractions</p> <p>Use of 1 – method ‘with replacement’ SC1 for $3 \times \frac{12}{50} \times \frac{12}{50} \times \frac{38}{50}$ SC2 for whole of $1 - 3 \times \frac{12}{50} \times \frac{12}{50} \times \frac{38}{50} + \frac{12}{50} \times \frac{12}{50} \times \frac{12}{50}$ $(= 1 - (0.1313 + 0.0138) = 1 - 0.1451 = 0.8549)$</p>
		TOTAL	18	

NOTE RE OVER-SPECIFICATION OF ANSWERS

If answers are grossly over-specified (see instruction 8), deduct the final answer mark in every case. Probabilities should also be rounded to a sensible degree of accuracy. In general final non probability answers should not be given to more than 4 significant figures. Allow probabilities given to 5 sig fig. In general accept answers which are correct to 3 significant figures when given to 4 or 5 significant figures.