Paper Reference(s)

# 6665/01 **Edexcel GCE**

## Core Mathematics C3

# **Advanced Level**

Monday 24 January 2011 – Morning

Time: 1 hour 30 minutes

**Materials required for examination** 

**Items included with question papers** 

Mathematical Formulae (Pink)

Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation or integration, or have retrievable mathematical formulae stored in them.

#### **Instructions to Candidates**

Write the name of the examining body (Edexcel), your centre number, candidate number, the unit title (Core Mathematics C3), the paper reference (6665), your surname, initials and signature.

#### **Information for Candidates**

A booklet 'Mathematical Formulae and Statistical Tables' is provided.

Full marks may be obtained for answers to ALL questions.

The marks for the parts of questions are shown in round brackets, e.g. (2).

There are 8 questions in this question paper. The total mark for this paper is 75.

#### **Advice to Candidates**

You must ensure that your answers to parts of questions are clearly labelled. You must show sufficient working to make your methods clear to the Examiner. Answers without working may not gain full credit.

1.	(a) Express $7 \cos x - 24 \sin x$ in the form $R \cos (x + \alpha)$ where $R > 0$ and $0 < \alpha < \frac{\pi}{2}$ .	
	Give the value of $\alpha$ to 3 decimal places.	

(3)

(b) Hence write down the minimum value of  $7 \cos x - 24 \sin x$ .

**(1)** 

(c) Solve, for  $0 \le x < 2\pi$ , the equation

$$7\cos x - 24\sin x = 10$$
,

giving your answers to 2 decimal places.

**(5)** 

**2.** (*a*) Express

$$\frac{4x-1}{2(x-1)} - \frac{3}{2(x-1)(2x-1)}$$

as a single fraction in its simplest form.

**(4)** 

Given that

$$f(x) = \frac{4x-1}{2(x-1)} - \frac{3}{2(x-1)(2x-1)} - 2, \qquad x > 1,$$

(b) show that

$$f(x) = \frac{3}{2x - 1}.$$

**(2)** 

(c) Hence differentiate f(x) and find f'(2).

**(3)** 

**3.** Find all the solutions of

$$2\cos 2\theta = 1 - 2\sin \theta$$

in the interval  $0 \le \theta < 360^{\circ}$ .

**(6)** 

**4.** Joan brings a cup of hot tea into a room and places the cup on a table. At time t minutes after Joan places the cup on the table, the temperature,  $\theta$  °C, of the tea is modelled by the equation

$$\theta = 20 + Ae^{-kt}$$

where A and k are positive constants.

Given that the initial temperature of the tea was 90 °C,

(a) find the value of A.

**(2)** 

The tea takes 5 minutes to decrease in temperature from 90 °C to 55 °C.

(b) Show that  $k = \frac{1}{5} \ln 2$ .

**(3)** 

(c) Find the rate at which the temperature of the tea is decreasing at the instant when t = 10. Give your answer, in °C per minute, to 3 decimal places.

3

**(3)** 

5.

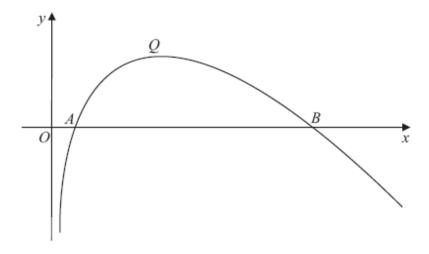


Figure 1

Figure 1 shows a sketch of part of the curve with equation y = f(x), where

$$f(x) = (8 - x) \ln x, \quad x > 0.$$

The curve cuts the x-axis at the points A and B and has a maximum turning point at Q, as shown in Figure 1.

(a) Write down the coordinates of A and the coordinates of B.

**(2)** 

(b) Find f'(x).

(3)

(c) Show that the x-coordinate of Q lies between 3.5 and 3.6

**(2)** 

(d) Show that the x-coordinate of Q is the solution of

$$x = \frac{8}{1 + \ln x} \,. \tag{3}$$

To find an approximation for the x-coordinate of Q, the iteration formula

$$x_{n+1} = \frac{8}{1 + \ln x_n}$$

4

is used.

(e) Taking  $x_0 = 3.55$ , find the values of  $x_1$ ,  $x_2$  and  $x_3$ . Give your answers to 3 decimal places.

**(3)** 

### **6.** The function f is defined by

f: 
$$x \mapsto \frac{3-2x}{x-5}$$
,  $x \in \mathbb{R}$ ,  $x \neq 5$ .

(a) Find  $f^{-1}(x)$ .

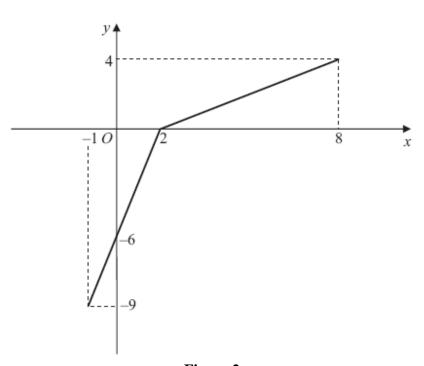


Figure 2

The function g has domain  $-1 \le x \le 8$ , and is linear from (-1, -9) to (2, 0) and from (2, 0) to (8, 4). Figure 2 shows a sketch of the graph of y = g(x).

(b) Write down the range of g.

**(1)** 

**(3)** 

**(2)** 

(
$$d$$
) Find fg(8).

**(2)** 

## (e) On separate diagrams, sketch the graph with equation

(i) 
$$y = |g(x)|$$
,

(ii) 
$$y = g^{-1}(x)$$
.

Show on each sketch the coordinates of each point at which the graph meets or cuts the axes. (4)

5

(f) State the domain of the inverse function  $g^{-1}$ .

**(1)** 

## **7.** The curve *C* has equation

$$y = \frac{3 + \sin 2x}{2 + \cos 2x}.$$

(a) Show that

$$\frac{dy}{dx} = \frac{6\sin 2x + 4\cos 2x + 2}{(2 + \cos 2x)^2}$$

**(4)** 

(b) Find an equation of the tangent to C at the point on C where  $x = \frac{\pi}{2}$ .

Write your answer in the form y = ax + b, where a and b are exact constants.

**(4)** 

### **8.** Given that

$$\frac{\mathrm{d}}{\mathrm{d}x}(\cos x) = -\sin x,$$

(a) show that  $\frac{d}{dx}(\sec x) = \sec x \tan x$ .

(3)

Given that

$$x = \sec 2y$$
,

(b) find  $\frac{dx}{dy}$  in terms of y.

**(2)** 

(c) Hence find  $\frac{dy}{dx}$  in terms of x.

**(4)** 

**TOTAL FOR PAPER: 75 MARKS** 

**END** 



# January 2011 Core Mathematics C3 6665 Mark Scheme

Question Number	Scheme		Mar	ks
1. (a)	$7\cos x - 24\sin x = R\cos(x+\alpha)$			
	$7\cos x - 24\sin x = R\cos x\cos\alpha - R\sin x\sin\alpha$			
	Equate $\cos x$ : $7 = R\cos\alpha$			
	Equate $\sin x$ : $24 = R \sin \alpha$			
	$R = \sqrt{7^2 + 24^2} \; ; = 25$	R=25	B1	
	$\tan \alpha = \frac{24}{7} \implies \alpha = 1.287002218^{c}$	$\tan \alpha = \frac{24}{7}$ or $\tan \alpha = \frac{7}{24}$	M1	
		awrt 1.287	A1	
	Hence, $7\cos x - 24\sin x = 25\cos(x + 1.287)$			(3)
(b)	Minimum value = $-25$	-25  or  -R	B1ft	
				(1)
(c)	$7\cos x - 24\sin x = 10$			
	$25\cos(x+1.287) = 10$			
	$\cos\left(x+1.287\right) = \frac{10}{25}$	$\cos(x \pm \text{their } \alpha) = \frac{10}{(\text{their } R)}$	M1	
	PV = 1.159279481° or 66.42182152°	For applying $\cos^{-1}\left(\frac{10}{\text{their }R}\right)$	M1	
	So, $x + 1.287 = \{1.159279^{c}, 5.123906^{c}, 7.442465^{c}\}$	either $2\pi + \text{or} - \text{their PV}^c \text{ or}$ $360^\circ + \text{or} - \text{their PV}^\circ$	M1	
	gives, $x = \{3.836906, 6.155465\}$	awrt 3.84 OR 6.16 awrt 3.84 AND 6.16	A1 A1	
		awit 5.07 / 111D 0.10	, , ,	(5) <b>[9]</b>
				- <b>-</b>



Question Number	Scheme		Marks
2.			
(a)	$\frac{4x-1}{2(x-1)} - \frac{3}{2(x-1)(2x-1)}$		
	$= \frac{(4x-1)(2x-1)-3}{2(x-1)(2x-1)}$ $8x^2 - 6x - 2$	An attempt to form a single fraction Simplifies to give a correct	M1
	$= \frac{8x^2 - 6x - 2}{\left\{2(x-1)(2x-1)\right\}}$	quadratic numerator over a correct quadratic denominator	A1 aef
	$= \frac{2(x-1)(4x+1)}{\left\{2(x-1)(2x-1)\right\}}$	An attempt to factorise a 3 term quadratic numerator	M1
	$= \frac{4x+1}{2x-1}$		A1 (4)
(b)	$f(x) = \frac{4x-1}{2(x-1)} - \frac{3}{2(x-1)(2x-1)} - 2,  x > 1$		
	$f(x) = \frac{(4x+1)}{(2x-1)} - 2$		
	$= \frac{(4x+1) - 2(2x-1)}{(2x-1)}$ $4x+1-4x+2$	An attempt to form a single fraction	M1
	$=\frac{4x+1-4x+2}{(2x-1)}$		
	$=\frac{3}{(2x-1)}$	Correct result	A1 * (2)
(c)	$f(x) = \frac{3}{(2x-1)} = 3(2x-1)^{-1}$		
	$f'(x) = 3(-1)(2x - 1)^{-2}(2)$	$\pm k (2x-1)^{-2}$	M1
			AT aer
	$f'(2) = \frac{-6}{9} = -\frac{2}{3}$	Either $\frac{-6}{9}$ or $-\frac{2}{3}$	
			(3) [9]



Question Number	Scheme		Marks
3.	$2\cos 2\theta = 1 - 2\sin \theta$		
	$2(1-2\sin^2\theta)=1-2\sin\theta$	Substitutes either $1 - 2\sin^2 \theta$ or $2\cos^2 \theta - 1$ or $\cos^2 \theta - \sin^2 \theta$ for $\cos 2\theta$ .	M1
	$2 - 4\sin^2\theta = 1 - 2\sin\theta$		
	$4\sin^2\theta - 2\sin\theta - 1 = 0$	Forms a "quadratic in sine" = 0	M1(*)
	$\sin \theta = \frac{2 \pm \sqrt{4 - 4(4)(-1)}}{8}$	Applies the quadratic formula See notes for alternative methods.	M1
	PVs: $\alpha_1 = 54^{\circ}$ or $\alpha_2 = -18^{\circ}$ $\theta = \{54, 126, 198, 342\}$	Any one correct answer 180-their pv All four solutions correct.	



Question Number	Scheme		Marks
4.	$\theta = 20 + Ae^{-kt}  (eqn *)$		
	$\{t = 0, \theta = 90 \Rightarrow\}  90 = 20 + Ae^{-k(0)}$	Substitutes $t = 0$ and $\theta = 90$ into eqn *	M1
	$90 = 20 + A \implies \underline{A = 70}$	<u>A = 70</u>	A1 (2)
(b)	$\theta = 20 + 70e^{-kt}$		
	$\{t = 5, \theta = 55 \implies\}  55 = 20 + 70e^{-k(5)}$ $\frac{35}{70} = e^{-5k}$	Substitutes $t = 5$ and $\theta = 55$ into eqn * and rearranges eqn * to make $e^{\pm 5k}$ the subject.	M1
	$ \ln\left(\frac{35}{70}\right) = -5k $	Takes 'lns' and proceeds to make ' $\pm 5k$ ' the subject.	dM1
	$-5k = \ln\left(\frac{1}{2}\right)$		
	$-5k = \ln 1 - \ln 2 \implies -5k = -\ln 2 \implies \underline{k = \frac{1}{5} \ln 2}$	Convincing proof that $k = \frac{1}{5} \ln 2$	A1 * (3)
(c)	$\theta = 20 + 70e^{-\frac{1}{5}t\ln 2}$		
	$\frac{d\theta}{dt} = -\frac{1}{5} \ln 2.(70) e^{-\frac{1}{5}t \ln 2}$	$\pm \alpha e^{-kt}$ where $k = \frac{1}{5} \ln 2$ -14 \ln 2 e^{-\frac{1}{5}t \ln 2}	M1 A1 oe
	When $t = 10$ , $\frac{d\theta}{dt} = -14 \ln 2 e^{-2 \ln 2}$		
	$\frac{\mathrm{d}\theta}{\mathrm{d}t} = -\frac{7}{2}\ln 2 = -2.426015132$		
	Rate of decrease of $\theta = 2.426 ^{\circ} C / \text{min}$ (3 dp.)	awrt ± 2.426	A1 (3) [8]



Question Number	Scheme		Ма	rks
5. (a)	Crosses x-axis $\Rightarrow$ f(x) = 0 $\Rightarrow$ (8 - x)ln x = 0			
	Either $(8 - x) = 0$ or $\ln x = 0 \Rightarrow x = 8, 1$ Either one of $\{x\}=1$ OR $x=0$	={8}	B1	
	Coordinates are $A(1, 0)$ and $B(8, 0)$ . Both $A(1, \{0\})$ and $B(8, 0)$ .	{0})	B1	(0)
				(2)
(b)	Apply product rule: $\begin{cases} u = (8 - x) & v = \ln x \\ \frac{du}{dx} = -1 & \frac{dv}{dx} = \frac{1}{x} \end{cases}$	+ <i>uv'</i>	M1	
	$f'(x) = -\ln x + \frac{8-x}{x}$ Any one term co	rrect	A1	
	Both terms co	rrect	A1	(3)
(c)	f'(3.5) = 0.032951317 f'(3.6) = -0.058711623 Attempts to evaluate Sign change (and as $f'(x)$ is continuous) therefore $f'(3.5)$ and $f'(3.5)$		M1	
	the <i>x</i> -coordinate of <i>Q</i> lies between 3.5 and 3.6.  both values correct to at least sign change and conclu		A1	(2)
(d)	At $Q$ , $f'(x) = 0 \implies -\ln x + \frac{8-x}{x} = 0$ Setting $f'(x)$	= 0.	M1	
	$\Rightarrow -\ln x + \frac{8}{x} - 1 = 0$ Splitting up the nume and proceeding t		M1	
	$\Rightarrow \frac{8}{x} = \ln x + 1 \Rightarrow 8 = x(\ln x + 1)$			
	$\Rightarrow x = \frac{8}{\ln x + 1}$ (as required) For correct p No errors seen in work		A1	(3)



Question Number	Scheme		Marks
(e)	Iterative formula: $x_{n+1} = \frac{8}{\ln x_n + 1}$		
	$x_1 = \frac{8}{\ln(3.55) + 1}$ $x_1 = 3.528974374$ $x_2 = 3.538246011$ $x_3 = 3.534144722$	An attempt to substitute $x_0 = 3.55$ into the iterative formula. Can be implied by $x_1 = 3.528(97)$ Both $x_1 = \text{awrt } 3.529$ and $x_2 = \text{awrt } 3.538$	M1 A1
	$x_1 = 3.529$ , $x_2 = 3.538$ , $x_3 = 3.534$ , to 3 dp.	$x_1$ , $x_2$ , $x_3$ all stated correctly to 3 dp	A1 (3) [13]



Question Number	Scheme		Marks
6. (a)	$y = \frac{3 - 2x}{x - 5} \implies y(x - 5) = 3 - 2x$	Attempt to make <i>x</i> (or swapped <i>y</i> ) the subject	M1
	xy - 5y = 3 - 2x	Collect <i>x</i> terms together and	
	$\Rightarrow xy + 2x = 3 + 5y \Rightarrow x(y+2) = 3 + 5y$	factorise.	M1
	$\Rightarrow x = \frac{3+5y}{y+2} \qquad \therefore f^{-1}(x) = \frac{3+5x}{x+2}$	$\frac{3+5x}{x+2}$	A1 oe (3)
(b)	Range of g is $-9 \le g(x) \le 4$ or $-9 \le y \le 4$	Correct Range	B1 (1)
(c)		Deduces that g(2) is 0. Seen or implied.	M1
	g g(2)=g(0) = -6, from sketch.	-6	A1 (2)
(d)	fg(8) = f(4)	Correct order g followed by f	M1
	$=\frac{3-4(2)}{4-5}=\frac{-5}{-1}=\underline{5}$	5	A1
			(2)



Question Number	Scheme	Marks
(e)(ii)	Correct shape	B1
	Graph goes through $(\{0\}, 2)$ and $(-6, \{0\})$ which are marked.	B1
		(4)
(f)	Domain of $g^{-1}$ is $-9 \le x \le 4$ Either correct answer or a follow through from part (b) answer	B1√ (1) [13]



Question Number	Scheme		Mar	ks
7				
(a)	$y = \frac{3 + \sin 2x}{2 + \cos 2x}$			
	Apply quotient rule: $\begin{cases}  u = 3 + \sin 2x & v = 2 + \cos 2x \\  \frac{du}{dx} = 2\cos 2x & \frac{dv}{dx} = -2\sin 2x \end{cases}$			
	$\frac{1}{2} = \frac{2}{2} = \frac{2}$	Applying $\frac{vu^r - uv^t}{v^2}$	M1	
	$\frac{dy}{dx} = \frac{2\cos 2x(2 + \cos 2x) - 2\sin 2x(3 + \sin 2x)}{(2 + \cos 2x)^2}$	Any one term correct on the	A1	
	(2 + cos 2x)	numerator Fully correct (unsimplified).	A1	
	$= \frac{4\cos 2x + 2\cos^2 2x + 6\sin 2x + 2\sin^2 2x}{(2+\cos 2x)^2}$			
	$= \frac{4\cos 2x + 6\sin 2x + 2(\cos^2 2x + \sin^2 2x)}{(2 + \cos 2x)^2}$	For correct proof with an understanding		
	$4\cos 2x + 6\sin 2x + 2$	that $\cos^2 2x + \sin^2 2x = 1$ .		
	$= \frac{4\cos 2x + 6\sin 2x + 2}{(2 + \cos 2x)^2}$ (as required)	No errors seen in working.	A1*	
	,			(4)
(b)	When $x = \frac{\pi}{2}$ , $y = \frac{3 + \sin \pi}{2 + \cos \pi} = \frac{3}{1} = 3$	<i>y</i> = 3	B1	
	At			
	$\left(\frac{\pi}{2}, 3\right),  m(\mathbf{T}) = \frac{6\sin\pi + 4\cos\pi + 2}{\left(2 + \cos\pi\right)^2} = \frac{-4 + 2}{1^2} = -2$	$m(\mathbf{T}) = -2$	B1	
	Either T: $y-3 = -2(x-\frac{\pi}{2})$	$y - y_1 = m(x - \frac{\pi}{2})$ with 'their		
	or $y = -2x + c$ and	TANGENT gradient' and their $y_1$ ;	M1	
	$3 = -2\left(\frac{\pi}{2}\right) + c \implies c = 3 + \pi ;$	or uses $y = mx + c$ with 'their TANGENT gradient';		
	<b>T:</b> $y = -2x + (\pi + 3)$	$y = -2x + \pi + 3$	A1	
				(4) [8]



8.  (a) $y = \sec x = \frac{1}{\cos x} = (\cos x)^{-1}$ Writes $\sec x$ as $(\cos x)^{-1}$ and gives $\frac{dy}{dx} = -1(\cos x)^{-2}(-\sin x)$ $\frac{dy}{dx} = -1(\cos x)^{-2}(-\sin x)$ $\frac{dy}{dx} = \left\{\frac{\sin x}{\cos^2 x}\right\} = \left(\frac{1}{\cos x}\right)\left(\frac{\sin x}{\cos x}\right) = \frac{\sec x \tan x}{\cos x}$ Convincing proof. Must see both underlined steps.  A1 AG  (b) $x = \sec 2y,  y \neq (2n+1)\frac{\pi}{4}, n \in \mathbb{Z}$ . $\frac{dx}{dy} = 2\sec 2y \tan 2y$ $\frac{dx}{dy} = 2\sec 2y \tan 2y$ Applies $\frac{dy}{dx} = \frac{1}{2\sec 2y \tan 2y}$ M1 $\frac{dy}{dx} = \frac{1}{2x \tan 2y}$ Applies $\frac{dy}{dx} = \frac{1}{(\frac{4\pi}{6y})}$ M1 $1 + \tan^2 A = \sec^2 A \Rightarrow \tan^2 2y = \sec^2 2y - 1$ Attempts to use the identity $1 + \tan^2 A = \sec^2 A$ M1  So $\tan^2 2y = x^2 - 1$ $\frac{dy}{dx} = \frac{1}{2x\sqrt{(x^2-1)}}$ A1  A1  (4)	Question	Scheme	М	arks
(a) $y = \sec x = \frac{1}{\cos x} = (\cos x)^{-1}$ Writes $\sec x$ as $(\cos x)^{-1}$ and gives $\frac{dy}{dx} = -1(\cos x)^{-2}(-\sin x)$ $\frac{dy}{dx} = -1(\cos x)^{-2}(-\sin x)$ $\frac{dy}{dx} = \frac{1}{\cos^{2}x} = \frac{1}{\cos^{2}x} = \frac{1}{\cos x} = \frac{1}{\cos $	Number			
$\frac{dy}{dx} = -1(\cos x)^{-2}(-\sin x) \qquad \frac{dy}{dx} = \pm ((\cos x)^{-2}(\sin x)) \qquad \text{A1}$ $\frac{dy}{dx} = \left\{\frac{\sin x}{\cos^{2} x}\right\} = \underbrace{\left(\frac{1}{\cos x}\right)\left(\frac{\sin x}{\cos x}\right)}_{\cos x} = \underbrace{\sec x \tan x}_{\cos x} \qquad \underbrace{\text{Convincing proof.}}_{\text{Must see both } \underline{\text{underlined steps.}}} \qquad \text{A1 AG}$ $\frac{dx}{dy} = 2\sec 2y \tan 2y \qquad \qquad 2\sec 2y \tan 2y \qquad \qquad 4 \qquad \qquad 4$		$y = \sec x = \frac{1}{\cos x} = (\cos x)^{-1}$		
$\frac{dx}{dx} = \frac{1}{\cos^2 x} = \frac{\cos x}{\cos x} = \frac{\sec x \tan x}{\cos x}$ Must see both underlined steps.  (3)  (b) $x = \sec 2y,  y \neq (2n+1)\frac{\pi}{4}, n \in \mathbb{Z}$ . $\frac{dx}{dy} = 2\sec 2y \tan 2y$ $2\sec 2y \tan 2y$ $2\sec 2y \tan 2y$ $4n = \frac{1}{2\sec 2y \tan 2y}$ M1 A1 $\frac{dy}{dx} = \frac{1}{2x \tan 2y}$ Applies $\frac{dy}{dx} = \frac{1}{\left(\frac{dx}{dy}\right)}$ M1 $1 + \tan^2 A = \sec^2 A \Rightarrow \tan^2 2y = \sec^2 2y - 1$ Attempts to use the identity $1 + \tan^2 A = \sec^2 A$ So $\tan^2 2y = x^2 - 1$ $\frac{dy}{dx} = \frac{1}{2x\sqrt{(x^2 - 1)}}$ A1		$\frac{\mathrm{d}y}{\mathrm{d}x} = -1(\cos x)^{-2}(-\sin x)$ $\frac{\mathrm{d}y}{\mathrm{d}x} = \pm \left((\cos x)^{-2}(\sin x)\right)$		
$\frac{dx}{dy} = 2\sec 2y \tan 2y$ $\frac{dy}{dx} = \frac{1}{2\sec 2y \tan 2y}$ $\frac{dy}{dx} = \frac{1}{2x \tan 2y}$ $1 + \tan^2 A = \sec^2 A \Rightarrow \tan^2 2y = \sec^2 2y - 1$ $\frac{dy}{dx} = \frac{1}{2x\sqrt{(x^2 - 1)}}$ $Applies \frac{dy}{dx} = \frac{1}{\left(\frac{dx}{dy}\right)}$ $Substitutes x \text{ for } \sec 2y.$ $Attempts \text{ to use the identity } 1 + \tan^2 A = \sec^2 A$ $\frac{dy}{dx} = \frac{1}{2x\sqrt{(x^2 - 1)}}$ $Attempts \text{ to use the identity } 1 + \tan^2 A = \sec^2 A$ $\frac{dy}{dx} = \frac{1}{2x\sqrt{(x^2 - 1)}}$ $A1$ $\frac{dy}{dx} = \frac{1}{2x\sqrt{(x^2 - 1)}}$ $A1$ $(4)$		$\frac{dy}{dx} = \left\{ \frac{\sin x}{\cos^2 x} \right\} = \underbrace{\left[ \frac{1}{\cos x} \right) \left( \frac{\sin x}{\cos x} \right)}_{\text{Cos } x} = \underbrace{\frac{\sec x \tan x}{\cos x}}_{\text{Must see both } \underline{\underline{\text{underlined steps.}}}}_{\text{Must see both } \underline{\underline{\text{underlined steps.}}}_{\text{Must see both } \underline{\underline{\text{underlined steps.}}}}_{\text{Must see both } \underline{\underline{\text{underlined steps.}}}_{\text{Must see both } \underline{\underline{\text{underlined steps.}}}}_{\text{Must see both } \underline{\underline{\text{underlined steps.}}}_{\text{Must see both } \underline{\text{un$	A1	<b>AG</b> (3)
$\frac{dy}{dx} = \frac{1}{2\sec 2y \tan 2y}$ $2\sec 2y \tan 2y$ $2\sec 2y \tan 2y$ $Applies \frac{dy}{dx} = \frac{1}{\left(\frac{dx}{dy}\right)}$ $\frac{dy}{dx} = \frac{1}{2x \tan 2y}$ $1 + \tan^2 A = \sec^2 A \Rightarrow \tan^2 2y = \sec^2 2y - 1$ $So \tan^2 2y = x^2 - 1$ $\frac{dy}{dx} = \frac{1}{2x\sqrt{(x^2 - 1)}}$ $Attempts to use the identity 1 + \tan^2 A = \sec^2 A$ $1 + \tan^2 A = \sec^2 A$ $\frac{dy}{dx} = \frac{1}{2x\sqrt{(x^2 - 1)}}$ $A1$ $A1$ $A1$	(b)	$x = \sec 2y$ , $y \neq (2n+1)\frac{\pi}{4}$ , $n \in \mathbb{Z}$ .		
$\frac{dy}{dx} = \frac{1}{2x \tan 2y}$ Substitutes $x$ for $\sec 2y$ . $1 + \tan^2 A = \sec^2 A \Rightarrow \tan^2 2y = \sec^2 2y - 1$ Attempts to use the identity $1 + \tan^2 A = \sec^2 A$ M1 $\frac{dy}{dx} = \frac{1}{2x\sqrt{(x^2 - 1)}}$ At $\frac{dy}{dx} = \frac{1}{2x\sqrt{(x^2 - 1)}}$ A1 $(4)$		$=2\sec 2v\tan 2v$		(2)
$1 + \tan^{2} A = \sec^{2} A \Rightarrow \tan^{2} 2y = \sec^{2} 2y - 1$ Attempts to use the identity $1 + \tan^{2} A = \sec^{2} A$ M1 $So \tan^{2} 2y = x^{2} - 1$ $\frac{dy}{dx} = \frac{1}{2x\sqrt{(x^{2} - 1)}}$ $A1$ (4)	(c)	$\frac{dy}{dx} = \frac{1}{2\sec 2y \tan 2y}$ Applies $\frac{dy}{dx} = \frac{1}{\left(\frac{dx}{dy}\right)}$	M1	
$1 + \tan^{2} A = \sec^{2} A \implies \tan^{2} 2y = \sec^{2} 2y - 1$ $1 + \tan^{2} A = \sec^{2} A$ $So \tan^{2} 2y = x^{2} - 1$ $\frac{dy}{dx} = \frac{1}{2x\sqrt{(x^{2} - 1)}}$ $A1$ $(4)$		$\frac{dy}{dx} = \frac{1}{2x \tan 2y}$ Substitutes x for sec 2y.	M1	
$\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{1}{2x\sqrt{(x^2 - 1)}} $ A1 (4)		$1 + ton^{-} A = coc^{-} A \implies ton^{-} A = coc^{-} A = 1$	M1	
(4)		So $\tan^2 2y = x^2 - 1$		
		$\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{1}{2x\sqrt{(x^2 - 1)}}$ $\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{1}{2x\sqrt{(x^2 - 1)}}$	A1	(4)
				[9]