

Paper Reference(s)

Paper 4 (Calculator) Higher Tier
Wednesday 12 November 2008 - Morning

## Materials required for examination

Ruler graduated in centimetres and millimetres, protractor, compasses, pen, HB pencil, eraser, calculator. Tracing paper may be used.

Items included with question papers
Nil

5540H/4H
Edexcel GCSE
Mathematics A (Linear) - 2540

Time: 1 hour 45 minutes


Team Leader's use only
$\square$

GCSE Mathematics (Linear) 2540

Formulae: Higher Tier
You must not write on this formulae page.
Anything you write on this formulae page will gain NO credit.

Volume of a prism $=$ area of cross section $\times$ length


Volume of sphere $=\frac{4}{3} \pi r^{3}$
Surface area of sphere $=4 \pi r^{2}$


In any triangle ABC


Volume of cone $=\frac{1}{3} \pi r^{2} h$
Curved surface area of cone $=\pi r l$


The Quadratic Equation
The solutions of $a x^{2}+b x+c=0$ where $a \neq 0$, are given by
$x=\frac{-b \pm \sqrt{\left(b^{2}-4 a c\right)}}{2 a}$

Sine Rule $\frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C}$
Cosine Rule $a^{2}=b^{2}+c^{2}-2 b c \cos A$

Area of triangle $=\frac{1}{2} a b \sin C$

## Answer ALL TWENTY SEVEN questions.

Write your answers in the spaces provided.
You must write down all stages in your working.

1. Here are the ingredients for making cheese pie for 6 people.

> Cheese pie for 6 people
> 180 g flour
> 240 g cheese
> 80 g butter
> 4 eggs
> $160 \mathrm{~m} l \mathrm{milk}$

Bill makes a cheese pie for 3 people.
(a) Work out how much flour he needs.

Jenny makes a cheese pie for 15 people.
(b) Work out how much milk she needs.
2. Use a calculator to work out

$$
\sqrt{\frac{21.6 \times 15.8}{3.8}}
$$

(a) Write down all the figures on your calculator display.
$\qquad$
(b) Give your answer to part (a) correct to 3 significant figures.
3. The cost of a radio is the list price plus VAT at $17 \frac{1}{2} \%$.

The list price of a radio is $£ 240$
Work out the cost of the radio.
4. (a) Expand $4(x-3)$
$\qquad$
(b) Solve
$4 t+1=19$

$$
t=
$$

5. The $n$th term of a sequence is $n^{2}+4$

Alex says
"The $n$th term of the sequence is always a prime number when $n$ is an odd number."
Alex is wrong.
Give an example to show that Alex is wrong.


A circle has a radius of 6 cm .

A square has a side of length 12 cm .
Work out the difference between the area of the circle and the area of the square.
Give your answer correct to one decimal place.

Diagram NOT accurately drawn
7.

Diagram NOT accurately drawn

$P Q$ is parallel to $R S$.
$O S Q$ and $O R P$ are straight lines.
(a) (i) Write down the value of $x$.

$$
x=
$$

$\qquad$
(ii) Give a reason for your answer.
$\qquad$
(b) Work out the value of $y$.
$\qquad$
8. Some students revised for a mathematics exam.

They used an internet revision site.
The scatter graph shows the times seven students spent on the internet revision site and the marks the students got in the mathematics exam.


Here is the information for 3 more students.

| Hours on the site | 7 | 10 | 16 |
| :--- | :---: | :---: | :---: |
| Mark | 50 | 56 | 78 |

(a) Plot this information on the scatter graph.
(b) What type of correlation does this scatter graph show?
$\qquad$
(c) Draw a line of best fit on the scatter graph.

A student spent 11 hours on the internet revision site.
(d) Use the line of best fit to estimate this student's mathematics exam mark.
$\qquad$
9. Jack invests $£ 3000$ for 2 years at $4 \%$ per annum compound interest.

Work out the value of the investment at the end of 2 years.

## $£$

$\qquad$
10. Jason collected some information about the heights of 19 plants.

This information is shown in the stem and leaf diagram.


Find the median.
mm
11. (a) Complete the table of values for $y=x^{2}-4 x-2$

| $x$ | -1 | 0 | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ |  | -2 | -5 |  |  | -2 | 3 |

(b) On the grid, draw the graph of $\quad y=x^{2}-4 x-2$

(c) Use your graph to estimate the values of $x$ when $y=-3$
$\qquad$

$$
x=
$$

$$
x=.
$$

12. (a) Draw the locus of all points which are equidistant from the points $A$ and $B$.

$$
A \times
$$

$$
\times B
$$

(b) Draw the locus of all points that are exactly 3 cm from the line $P Q$.

```
P
Q
```

(2) Q12
13. Find the Lowest Common Multiple (LCM) of 24 and 36
14. (a) Expand and simplify $3(x+4)+5(2 x+1)$
(b) Simplify $t^{4} \times t^{6}$
$\qquad$
(c) Simplify $p^{8} \div p^{5}$
$\qquad$
(d) Simplify $\quad\left(x^{4}\right)^{3}$
15. Here is a 5 -sided spinner.


The sides of the spinner are labelled 1,2,3, 4 and 5
The spinner is biased.
The probability that the spinner will land on each of the numbers $1,2,3$ and 4 is given in the table.

| Number | 1 | 2 | 3 | 4 | 5 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Probability | 0.15 | 0.05 | 0.2 | 0.25 | $x$ |

Work out the value of $x$.

$$
x=
$$

16. 

Diagram NOT accurately drawn


In triangle $A B C$,
$A B=10 \mathrm{~cm}$
$A C=20 \mathrm{~cm}$
angle $B A C=90^{\circ}$
Work out the length of $B C$.
Give your answer correct to 3 significant figures.
You must state the units in your answer.
17. Majid carried out a survey of the number of school dinners 32 students had in one week. The table shows this information.

| Number of school dinners | Frequency |  |
| :---: | :---: | :--- |
| 0 | 0 |  |
| 1 | 8 |  |
| 2 | 12 |  |
| 3 | 6 |  |
| 4 | 4 |  |
| 5 | 2 |  |

Calculate the mean.
18. The value of a car depreciates by $35 \%$ each year.

At the end of 2007 the value of the car was $£ 5460$
Work out the value of the car at the end of 2006
$\qquad$
19. The diagram below shows a 6 -sided shape.

All the corners are right angles.
All the measurements are given in centimetres.
Diagram NOT
accurately drawn


The area of the shape is $95 \mathrm{~cm}^{2}$.
(a) Show that
$2 x^{2}+6 x-95=0$
(b) Solve the equation

$$
2 x^{2}+6 x-95=0
$$

Give your solutions correct to 3 significant figures.
$\qquad$ or $x=$
20. The $n$th even number is $2 n$.

The next even number after $2 n$ is $2 n+2$
(a) Explain why.
$\qquad$
$\qquad$
(b) Write down an expression, in terms of $n$, for the next even number after $2 n+2$
$\qquad$
(c) Show algebraically that the sum of any 3 consecutive even numbers is always a multiple of 6
21.

Diagram NOT
accurately drawn

$P Q R$ is a right-angled triangle.
$Q R=4 \mathrm{~cm}$
$P R=10 \mathrm{~cm}$
Work out the size of angle $R P Q$.
Give your answer correct to 3 significant figures.
22. $D$ is proportional to $S^{2}$.
$D=900$ when $S=20$
Calculate the value of $D$ when $S=25$

$$
D=
$$

23. A ball is thrown vertically upwards with a speed $V$ metres per second.

The height, $H$ metres, to which it rises is given by

$$
H=\frac{V^{2}}{2 g}
$$

where $g \mathrm{~m} / \mathrm{s}^{2}$ is the acceleration due to gravity.
$V=24.4$ correct to 3 significant figures.
$g=9.8$ correct to 2 significant figures.
(i) Write down the lower bound of $g$.
(ii) Calculate the upper bound of $H$.

Give your answer correct to 3 significant figures.
$\qquad$


The storage tank consists of a hemisphere on top of a cylinder.
The height of the cylinder is 30 metres.
The radius of the cylinder is 3 metres.
The radius of the hemisphere is 3 metres.
(a) Calculate the total volume of the storage tank.

Give your answer correct to 3 significant figures.

A sphere has a volume of $500 \mathrm{~m}^{3}$.
(b) Calculate the radius of the sphere.

Give your answer correct to 3 significant figures.
25.

|  | Male | Female |
| :--- | :---: | :---: |
| First year | 399 | 602 |
| Second year | 252 | 198 |

The table gives information about the numbers of students in the two years of a college course.

Anna wants to interview some of these students.
She takes a random sample of 70 students stratified by year and by gender.
Work out the number of students in the sample who are male and in the first year.
$\qquad$
26.


$$
\begin{aligned}
& \overrightarrow{O X}=2 \mathbf{a}+\mathbf{b} \\
& \overrightarrow{O Y}=4 \mathbf{a}+3 \mathbf{b}
\end{aligned}
$$

(a) Express the vector $\overrightarrow{X Y}$ in terms of $\mathbf{a}$ and $\mathbf{b}$ Give your answer in its simplest form.

Diagram NOT
accurately drawn


Diagram NOT accurately drawn
$X Y Z$ is a straight line.
$X Y: Y Z=2: 3$
(b) Express the vector $\overrightarrow{O Z}$ in terms of $\mathbf{a}$ and $\mathbf{b}$ Give your answer in its simplest form.
27.


The diagram shows a sketch of the graph $\quad y=a b^{x}$
The curve passes through the points $A(0.5,1)$ and $B(2,8)$.
The point $C(-0.5, k)$ lies on the curve.
Find the value of $k$.

END

