

Paper Reference(s)

# 5525/06 <br> Edexcel GCSE Mathematics A-1387 <br> Paper 6 (Calculator) Higher Tier 



Examiner's use only


Team Leader's use only
$\square$

Friday 9 November 2007 - Morning
Time: 2 hours

## Materials required for examination

Ruler graduated in centimetres and millimetres, protractor, compasses, pen, HB pencil, eraser, calculator. Tracing paper may be used.

## Instructions to Candidates

In the boxes above, write your centre number, candidate number, your surname, initials and signature. Check that you have the correct question paper.
Answer ALL the questions in the spaces provided in this question paper.
You must NOT write on the formulae page. Anything you write on the formulae page will gain NO credit.
If you need more space to complete your answer to any question, use additional answer sheets.

## Information for Candidates

The marks for individual questions and the parts of questions are shown in round brackets: e.g. (2). There are 25 questions in this question paper. The total mark for this paper is 100 .
There are 24 pages in this question paper. Any blank pages are indicated.
Calculators may be used.
If your calculator does not have a $\pi$ button, take the value of $\pi$ to be 3.142 unless the question instructs otherwise.

## Advice to Candidates

Show all stages in any calculations.
Work steadily through the paper. Do not spend too long on one question.
If you cannot answer a question, leave it and attempt the next one.
Return at the end to those you have left out.

## GCSE Mathematics 1387/8

Formulae: Higher Tier
You must not write on this formulae page.
Anything you write on this formulae page will gain NO credit.

Volume of a prism $=$ area of cross section $\times$ length


Volume of sphere $=\frac{4}{3} \pi r^{3}$
Surface area of sphere $=4 \pi r^{2}$


In any triangle ABC


Sine Rule $\frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C}$
Cosine Rule $a^{2}=b^{2}+c^{2}-2 b c \cos A$

Area of triangle $=\frac{1}{2} a b \sin C$

Volume of cone $=\frac{1}{3} \pi r^{2} h$
Curved surface area of cone $=\pi r l$


The Quadratic Equation
The solutions of $a x^{2}+b x+c=0$ where $a \neq 0$, are given by

$$
x=\frac{\left.-b \pm \sqrt{\left(b^{2}-4 a c\right.}\right)}{2 a}
$$

## Answer ALL TWENTY FIVE questions.

Write your answers in the spaces provided.

## You must write down all stages in your working.

1. In April 2004, the population of the European Community was 376 million.

In April 2005, the population of the European Community was 451 million.
Work out the percentage increase in population.
Give your answer correct to 1 decimal place.
2. The equation

$$
x^{3}-5 x=60
$$

has a solution between 4 and 5 .
Use a trial and improvement method to find this solution.
Give your answer correct to 1 decimal place.
You must show all your working.

## Diagram NOT

 accurately drawnIn the triangle $X Y Z$
$X Y=5.6 \mathrm{~cm}$
$Y Z=10.5 \mathrm{~cm}$
angle $X Y Z=90^{\circ}$
(a) Work out the length of $X Z$.


Diagram NOT accurately drawn

4 copies of the triangle are fitted together to make the shape shown in the diagram.
(b) Calculate the perimeter of the shape.
4.

Diagram NOT
accurately drawn


The diagram shows a semicircle.
The radius of the semicircle is 10 cm .
Calculate the area of the semicircle.
Give your answer correct to 3 significant figures.
State the units of your answer.
5. The table gives information about the times, in minutes, that 106 shoppers spent in a supermarket.

| Time ( $t$ minutes) | Frequency |  |
| :---: | :---: | :--- |
| $0<t \leqslant 10$ | 20 |  |
| $10<t \leqslant 20$ | 17 |  |
| $20<t \leqslant 30$ | 12 |  |
| $30<t \leqslant 40$ | 32 |  |
| $40<t \leqslant 50$ | 25 |  |

(a) Find the class interval that contains the median.
(b) Calculate an estimate for the mean time that the shoppers spent in the supermarket. Give your answer correct to 3 significant figures.
minutes
(4)
6. (a) Complete the table of values for $y=2 x^{2}-4 x$

| $x$ | -2 | -1 | 0 | 1 | 2 | 3 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ | 16 |  | 0 |  |  | 6 |

(b) On the grid, draw the graph of $y=2 x^{2}-4 x$ for values of $x$ from -2 to 3

(c) (i) On the same axes, draw the straight line $y=2.5$
(ii) Write down the values of $x$ for which $2 x^{2}-4 x=2.5$
7. On July 1st 2004, Jack invested $£ 2000$ at $5 \%$ per annum compound interest.

Work out the value of Jack's investment on July 1st 2006
$\qquad$
8. Write 720 as a product of its prime factors.
$\qquad$
9. Simplify
(a) $p^{7} \times p^{9}$
$\qquad$

Simplify (b) $\frac{q^{12} \times q^{4}}{q^{6}}$
10. In a sale, normal prices are reduced by $25 \%$.

The sale price of a saw is $£ 12.75$
Calculate the normal price of the saw.
£ $\qquad$
11. Work out

$$
\frac{2 \times 2.2 \times 10^{12} \times 1.5 \times 10^{12}}{2.2 \times 10^{12}-1.5 \times 10^{12}}
$$

Give your answer in standard form correct to 3 significant figures.
$\qquad$
12. Solve

$$
\begin{aligned}
& 3 x+y=8 \\
& 4 x+2 y=9
\end{aligned}
$$

$x=$ $\qquad$
$y=$ $\qquad$
13.


Diagram NOT accurately drawn
(a) In the diagram, $O$ is the centre of the circle.
$A, B$ and $C$ are points on the circle.
Angle $C O A=130^{\circ}$.
(i) Find the size of angle $C B A$.
(ii) Give a reason for your answer.
$\qquad$
$\qquad$


Diagram NOT
accurately drawn
(b) In the diagram, $O$ is the centre of the circle.
$P, Q, R$ and $S$ are points on the circle.
Angle $R O P=110^{\circ}$
Calculate the size of angle $R S P$.
14.

Diagram NOT accurately drawn

$P Q R$ is a right-angled triangle.
$P R=12 \mathrm{~cm}$.
$Q R=4.5 \mathrm{~cm}$.
Angle $P R Q=90^{\circ}$.
Work out the value of $x$.
Give your answer correct to one decimal place.
15. $A=\frac{h(x+10)}{2}$
$A=27$
$h=4$

Work out the value of $x$.
16.

| Month | Jan | Feb | Mar | Apr | May | Jun |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Number of <br> Televisions | 1240 | 1270 | 1330 | 1300 | 1330 | $x$ |

The table shows the number of televisions sold in a shop in the first five months of 2006.
(a) Work out the first 3-month moving average for the information in the table.

The fourth 3-month moving average of the number of televisions sold in 2006 is 1350 The number of televisions sold in the shop in June was $x$.
(b) Work out the value of $x$.

$$
x=.
$$

$\qquad$
17. Julie has 100 music CDs.

58 of the CDs are classical.
22 of the CDs are folk.
The rest of the CDs are jazz.
On Saturday, Julie chooses one CD at random from the 100 CDs.
On Sunday, Julie chooses one CD at random from the 100 CDs.
(a) Complete the probability tree diagram.

(b) Calculate the probability that Julie will choose a jazz CD on both Saturday and Sunday.
(c) Calculate the probability that Julie will choose at least one jazz CD on Saturday and Sunday.
18. $f$ is inversely proportional to $d$.

When $d=50, f=256$
Find the value of $f$ when $d=80$
$f=$
19. The diagram shows a 6 -sided shape.

All the corners are right angles.
All the measurements are given in centimetres.


The area of the shape is $85 \mathrm{~cm}^{2}$.
(a) Show that $9 x^{2}-17 x-85=0$
(b) (i) Solve $9 x^{2}-17 x-85=0$

Give your solutions correct to 3 significant figures.

$$
x=
$$

$\qquad$ or $x=$ $\qquad$
(ii) Hence, work out the length of the shortest side of the 6 -sided shape.
20.

Diagram NOT
accurately drawn

$A B$ is parallel to $D C$.
$A D=9 \mathrm{~cm}, D C=3 \mathrm{~cm}$.
Angle $B C D=35^{\circ}$.
Angle $A B D=90^{\circ}$.
Calculate the size of angle $B A D$.
Give your answer correct to one decimal place.
21. The diagram shows an equilateral triangle.


Diagram NOT accurately drawn

The area of the equilateral triangle is $36 \mathrm{~cm}^{2}$.
Find the value of $x$.
Give your answer correct to 3 significant figures.
$x=$ $\qquad$
22. (a) Simplify $\left(2 x^{4} y^{5}\right)^{3}$
$\qquad$
$y=\frac{2 p t}{p-t}$
(b) Rearrange the formula to make $t$ the subject.

$$
t=
$$

$\qquad$
23. The mass $M$ grams of a cube with edges of length $L \mathrm{~cm}$ and density $D$ grams per $\mathrm{cm}^{3}$ is given by the formula

$$
M=D L^{3}
$$

$D=8$ correct to 1 significant figure.
$L=6.4$ correct to 1 decimal place.
Calculate the upper bound of $M$.
Give your answer correct to 2 significant figures.
$\qquad$
24. $x^{2}-8 x+23=(x-p)^{2}+q$ for all values of $x$.
(a) Find the value of $p$ and the value of $q$.

$$
0=.
$$

$\qquad$

Here is a sketch of the curve with equation $y=x^{2}-8 x+23$

$B$ is the minimum point on the curve.
(b) Find the coordinates of $B$.
$\qquad$

The equation of the curve can be written in the form $y=\mathrm{f}(x)$, where $\mathrm{f}(x)=x^{2}-8 x+23$
(c) On the diagram below, draw a sketch of the curve $y=\mathrm{f}(-x)$.

(1)

Diagram NOT
accurately drawn


The diagram shows a tetrahedron.
$A D$ is perpendicular to both $A B$ and $A C$.
$A B=10 \mathrm{~cm}$.
$A C=8 \mathrm{~cm}$.
$A D=5 \mathrm{~cm}$.
Angle $B A C=90^{\circ}$.
Calculate the size of angle $B D C$.
Give your answer correct to 1 decimal place.

