

## Paper Reference(s)

# 5525/05 <br> Edexcel GCSE Mathematics A-1387 <br> Paper 5 (Non-Calculator) Higher Tier 

Examiner's use only


Team Leader's use only
$\square$

Monday 4 June 2007 - Afternoon

Time: 2 hours

Materials required for examination Ruler graduated in centimetres and millimetres, protractor, compasses, pen, HB pencil, eraser. Tracing paper may be used. Items included with question papers

## Instructions to Candidates

In the boxes above, write your centre number, candidate number, your surname, initials and signature. Check that you have the correct question paper.
Answer ALL the questions. Write your answers in the spaces provided in this question paper.
You must NOT write on the formulae page. Anything you write on the formulae page will gain NO credit.
If you need more space to complete your answer to any question, use additional answer sheets.

## Information for Candidates

The marks for individual questions and the parts of questions are shown in round brackets: e.g. (2)
There are 27 questions in this question paper. The total mark for this paper is 100 .
There are 24 pages in this question paper. Any blank pages are indicated.
Calculators must not be used.

## Advice to Candidates

Show all stages in any calculations.
Work steadily through the paper. Do not spend too long on one question.
If you cannot answer a question, leave it and attempt the next one.
Return at the end to those you have left out.


## GCSE Mathematics 1387/8

Formulae: Higher Tier
You must not write on this formulae page.
Anything you write on this formulae page will gain NO credit.

Volume of a prism $=$ area of cross section $\times$ length


Volume of sphere $=\frac{4}{3} \pi r^{3}$
Surface area of sphere $=4 \pi r^{2}$


In any triangle ABC


Sine Rule $\frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C}$
Cosine Rule $a^{2}=b^{2}+c^{2}-2 b c \cos A$

Area of triangle $=\frac{1}{2} a b \sin C$

Volume of cone $=\frac{1}{3} \pi r^{2} h$
Curved surface area of cone $=\pi r l$


The Quadratic Equation
The solutions of $a x^{2}+b x+c=0$
where $a \neq 0$, are given by
$x=\frac{-b \pm \sqrt{\left(b^{2}-4 a c\right)}}{2 a}$

## Answer ALL TWENTY SEVEN questions.

Write your answers in the spaces provided.
You must write down all stages in your working.
You must NOT use a calculator.

1. A bag contains counters which are red or green or yellow or blue.

The table shows each of the probabilities that a counter taken at random from the bag will be red or green or blue.

| Colour | Red | Green | Yellow | Blue |
| :--- | :---: | :---: | :---: | :---: |
| Probability | 0.2 | 0.3 |  | 0.1 |

A counter is to be taken at random from the bag.
(a) Work out the probability that the counter will be yellow.

The bag contains 200 counters.
(b) Work out the number of red counters in the bag.
$\qquad$
(2)
2. Kate buys 2 lollies and 5 choc ices for $£ 6.50$

Pete buys 2 lollies and 3 choc ices for $£ 4.30$
Work out the cost of one lolly.
Give your answer in pence.
3. Matthew wants to collect information about the time students take to travel to school.

Design a suitable question he could use on a questionnaire.
4.


Work out the total surface area of the L-shaped prism.
State the units with your answer.
5. Work out the coordinates of the midpoint of the line joining the points $(4,5)$ and $(-6,3)$.

$(-6,3)$
$\qquad$
6. Mrs Raja set work for the students in her class.

She recorded the time taken, in minutes, for each student to do the work.
She used her results to work out the information in the table.

|  | Minutes |
| :--- | :---: |
| Shortest time | 4 |
| Lower quartile | 14 |
| Median | 26 |
| Upper quartile | 30 |
| Longest time | 57 |

On the grid, draw a box plot to show the information in the table.

7.


Use ruler and compasses to construct the bisector of angle $P Q R$.
You must show all your construction lines.
8. (a) Write 126 as a product of its prime factors.
(b) Find the Highest Common Factor (HCF) of 84 and 126
9. (a) $m$ is an integer such that $-1 \leqslant m<4$

List all the possible values of $m$.
(b) (i) Solve the inequality $3 x \geqslant x+7$
(ii) $x$ is a whole number.

Write down the smallest value of $x$ that satisfies $3 x \geqslant x+7$
10. (a) Write as a power of 7
(i) $7^{8} \div 7^{3}$
(ii) $\frac{7^{2} \times 7^{3}}{7}$
$\qquad$
(b) Write down the reciprocal of 2
11. (a) Make $n$ the subject of the formula $m=5 n-21$

$$
n=
$$

(b) Make $p$ the subject of the formula $4(p-2 q)=3 p+2$

$$
p=
$$

12. 



Diagram NOT accurately drawn

The straight line $\mathbf{L}$ has equation $y=\frac{1}{2} x+7$
The straight line $\mathbf{M}$ is parallel to $\mathbf{L}$ and passes through the point $(0,3)$.
Write down an equation for the line $\mathbf{M}$.
13. Work out $2 \frac{2}{3} \times 1 \frac{1}{4}$

Give your answer in its simplest form.
14. Solve the simultaneous equations

$$
\begin{aligned}
& 4 x+2 y=8 \\
& 2 x-5 y=10
\end{aligned}
$$

15. 


$A B C D E F$ is a regular hexagon and $A B Q P$ is a square.
Angle $C B Q=x^{\circ}$.
Work out the value of $x$.
16. An operator took 100 calls at a call centre.

The table gives information about the time ( $t$ seconds) it took the operator to answer each call.

| Time $(\boldsymbol{t}$ seconds) | Frequency |
| :---: | :---: |
| $0<t \leqslant 10$ | 16 |
| $10<t \leqslant 20$ | 34 |
| $20<t \leqslant 30$ | 32 |
| $30<t \leqslant 40$ | 14 |
| $40<t \leqslant 50$ | 4 |

(a) Complete the cumulative frequency table.

| Time $(\boldsymbol{t}$ seconds) | Cumulative frequency |
| :---: | :---: |
| $0<t \leqslant 10$ | 16 |
| $0<t \leqslant 20$ |  |
| $0<t \leqslant 30$ |  |
| $0<t \leqslant 40$ |  |
| $0<t \leqslant 50$ |  |


(b) On the grid, draw a cumulative frequency graph for your table.
(c) Use your graph to find an estimate for the number of calls the operator took more than 18 seconds to answer.
17. There are two sets of traffic lights on Georgina's route to school. The probability that the first set of traffic lights will be red is 0.4 The probability that the second set of traffic lights will be red is 0.3
(a) Complete the probability tree diagram.

(b) Work out the probability that both sets of traffic lights will be red.
(c) Work out the probability that exactly one set of traffic lights will be red.
18. Prove that the recurring decimal $0 . \dot{4} \dot{5}=\frac{15}{33}$
19. Expand and simplify $(\sqrt{3}-\sqrt{2})(\sqrt{3}+\sqrt{2})$
, Ex
20.

Diagrams NOT accurately drawn


Two cones, $\mathbf{P}$ and $\mathbf{Q}$, are mathematically similar.
The total surface area of cone $\mathbf{P}$ is $24 \mathrm{~cm}^{2}$.
The total surface area of cone $\mathbf{Q}$ is $96 \mathrm{~cm}^{2}$.
The height of cone $\mathbf{P}$ is 4 cm .
(a) Work out the height of cone $\mathbf{Q}$.

The volume of cone $\mathbf{P}$ is $12 \mathrm{~cm}^{3}$.
(b) Work out the volume of cone $\mathbf{Q}$.
21. (a) Expand $x\left(3-2 x^{2}\right)$
(b) Factorise completely $12 x y+4 x^{2}$
(c) Simplify $\frac{20 a^{2}}{4 a b^{2}}$
(d) Simplify $\frac{x-3}{x^{2}-9}$
22.

Diagram NOT
 accurately drawn
$A B C D E F$ is a regular hexagon.
$\overrightarrow{A B}=\mathbf{a} \quad \overrightarrow{B C}=\mathbf{b} \quad \overrightarrow{A D}=\mathbf{2} \mathbf{b}$
(a) Find the vector $\overrightarrow{A C}$ in terms of $\mathbf{a}$ and $\mathbf{b}$.

$$
\overrightarrow{A C}=
$$

$\qquad$
$\overrightarrow{A C}=\overrightarrow{C X}$
(b) Prove that $A B$ is parallel to $D X$.
23. The diagram shows a cylinder and a sphere.


The radius of the base of the cylinder is $2 x \mathrm{~cm}$ and the height of the cylinder is $h \mathrm{~cm}$. The radius of the sphere is $3 x \mathrm{~cm}$.
The volume of the cylinder is equal to the volume of the sphere.
Express $h$ in terms of $x$.
Give your answer in its simplest form.
24. (i) Expand and simplify

$$
n^{2}+(n+1)^{2}
$$

$n$ is a whole number.
(ii) Prove that $n^{2}+(n+1)^{2}$ is always an odd number.
25. Here is a graph of the curve $y=\cos x^{\circ}$ for $0 \leqslant x \leqslant 360$


Use the graph to solve $\cos x^{\circ}=0.75$ for $0 \leqslant x \leqslant 360$

26. For all values of $x$,

$$
x^{2}-6 x+15=(x-p)^{2}+q
$$

(a) Find the value of $p$ and the value of $q$.
(b) On the axes, draw a sketch of the graph $y=x^{2}-6 x+15$

(2)
27. The graph of $y=\mathrm{f}(x)$ is shown on the grids.
(a) On this grid, sketch the graph of $y=\mathrm{f}(x)+2$

(b) On this grid, sketch the graph of $y=-\mathrm{f}(x)$

(2) Q 27
(Total 4 marks)

