| Centre <br> No |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Candidate <br> No |  |  |  |  |  |

## 5506/06

Edexcel GCSE Mathematics A-1387
Paper 6 (Calculator)

## Higher Tier

# Tuesday 9 November 2004 - Morning Time: 2 hours 

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Materials required for examination
Ruler graduated in centimetres and
Items included with question papers
Nil millimetres, protractor, compasses, pen, HB pencil, eraser, calculator. Tracing paper may be used.
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## Instructions to Candidates

In the boxes above, write your centre number, candidate number, your surname, initials and signature. Check that you have the correct question paper.
Answer ALL the questions in the spaces provided in this question paper.
You must NOT write on the formulae page or any blank pages. Anything you write on these pages will gain NO credit.
If you need more space to complete your answer to any question, use additional answer sheets.

## Information for Candidates

The total mark for this paper is 100 . This paper has 22 questions. There are 3 blank pages.
The marks for individual questions and parts of questions are shown in round brackets: e.g. (2).
Calculators may be used.
If your calculator does not have a $\pi$ button, take the value of $\pi$ to be 3,142 unless the question instructs otherwise.

## Advice to Candidates

Show all stages in any calculations.
Work steadily through the paper. Do not spend too long on one question.
If you cannot answer a question, leave it and attempt the next one.
Return at the end to those you have left out.

## Answer ALL TWENTY TWO questions.

Write your answers in the spaces provided.

## You must write down all stages in your working.

1. 

|  | Number of girls | Number of boys |
| :---: | :---: | :---: |
| Year 10 | 108 | 132 |
| Year 11 | 90 | 110 |

The table gives information about Year 10 and Year 11 at Mathstown School.
Mathstown School had an end of term party.
$40 \%$ of the students in Year 10 and $70 \%$ of the students in Year 11 went to the party.
Work out the percentage of all students in Years 10 and 11 who went to the party.
$\qquad$
2. Pablo is an artist.

The scatter graph, opposite, gives information about the area and the cost of some of his pictures.
The line of best fit has been drawn on the graph.
All Pablo's pictures are rectangles.
One of his pictures costs $£ 1000$.
Its length is 48 cm .
Use the line of best fit to estimate the width of the picture.

(Total 2 marks)
3. The equation $x^{3}+4 x=100$
has one solution which is a positive number.
Use the method of trial and improvement to find this solution.
Give your answer correct to 1 decimal place.
You must show ALL your working.

$$
x=.
$$

4. (a) Solve $4(2 x+1)=2(3-x)$

$$
x=.
$$

$\qquad$
(b) Factorise fully

$$
2 p^{2}-4 p q
$$

(c) Factorise fully

$$
x^{2}+7 x+6
$$

5. Nicola invests $£ 8000$ for 3 years at $5 \%$ per annum compound interest.
(a) Calculate the value of her investment at the end of 3 years.
$\qquad$
£.. $\qquad$

Jim invests a sum of money for 30 years at $4 \%$ annum compound interest.




(b) Write down the letter of the graph which best shows how the value of Jim's investment changes over the 30 years.

Hannah invested an amount of money in an account paying $5 \%$ per annum compound interest.
After 1 year the value of her investment was $£ 3885$
(c) Work out the amount of money that Hannah invested.
$\qquad$
£..
(3)
(Total 7 marks)
6. Fred runs 200 metres in 21.2 seconds.
(a) Work out Fred's average speed.

Write down all the figures on your calculator display.
metres per second
(2)
(b) Round off your answer to part (a) to an appropriate degree of accuracy.
7. Tony throws a biased dice 100 times.

The table shows his results

| Score | Frequency |
| :---: | :---: |
| 1 | 12 |
| 2 | 13 |
| 3 | 17 |
| 4 | 10 |
| 5 | 18 |
| 6 | 30 |

He throws the dice once more.
(a) Find an estimate for the probability that he will get a 6 .

Emma has a biased coin.
The probability that the biased coin will land on a head is 0.7
Emma is going to throw the coin 250 times.
(b) Work out an estimate for the number of times the coin will land on a head.
8.


Diagram NOT accurately drawn
$P Q R$ is a triangle.
Angle $P Q R=90^{\circ}$.
$P Q=12.5 \mathrm{~cm}$.
$Q R=5 \mathrm{~cm}$.
Calculate the value of $x$.
Give your answer correct to 1 decimal place.
9.


Diagram NOT accurately drawn
$A B C D$ is a rectangle.
$A C=17 \mathrm{~cm}$.
$A D=10 \mathrm{~cm}$.
Calculate the length of the side $C D$.
Give your answer correct to one decimal place.
10.

$$
\sqrt{\frac{r+t \sin x^{\circ}}{r-t \sin x^{\circ}}}
$$

$r=8.8$
$t=7.2$
$x=40$
(a) Calculate the value of $y$. Give your answer correct to 3 significant figures.
$y=$
(3)
$y=2$
$t=10$
$x=30$
(b) Find the value of $r$.

$$
\begin{equation*}
r= \tag{3}
\end{equation*}
$$

(Total 6 marks)
11. The straight line $\mathbf{L}_{\mathbf{1}}$ has equation $y=2 x+3$

The straight line $\mathbf{L}_{\mathbf{2}}$ is parallel to the straight line $\mathbf{L}_{\mathbf{1}}$. The straight line $\mathbf{L}_{2}$ passes through the point (3, 2).

Find an equation of the straight line $\mathbf{L}_{\mathbf{2}}$.
12. A youth club has 60 members.

40 of the members are boys.
20 of the members are girls.
The mean number of videos watched last week by all 60 members was 2.8
The mean number of videos watched last week by the 40 boys was 3.3
(a) Calculate the mean number of videos watched last week by the 20 girls.

Ibrahim has two lists of numbers.
The mean of the numbers in the first list is $p$.
The mean of the numbers in the second list is $q$.
Ibrahim combines the two lists into one new list of numbers.

Ibrahim says 'The mean of the new list of numbers is equal to $\frac{p+q}{2}$.'

One of two conditions must be satisfied for Ibrahim to be correct.
(b) Write down each of these conditions.

Condition 1 $\qquad$
$\qquad$
Condition 2 $\qquad$
$\qquad$
13.


Diagram NOT accurately drawn
$B E$ is parallel to $C D$.
$A B C$ and $A E D$ are straight lines.
$A B=4 \mathrm{~cm}, B C=6 \mathrm{~cm}, B E=5 \mathrm{~cm}, A E=4.8 \mathrm{~cm}$.
(a) Calculate the length of $C D$.
(b) Calculate the length of $E D$.
14. (a) Solve $x^{2}+x+11=14$

Give your solutions correct to 3 significant figures.

$$
y=x^{2}+x+11
$$

The value of $y$ is a prime number when $x=0,1,2$ and 3
The following statement is not true.
$' y=x^{2}+x+11$ is always a prime number when $x$ is an integer'
(b) Show that the statement is not true.
$\qquad$
$\qquad$
15.


Diagram NOT accurately drawn

The diagram represents a cuboid $A B C D E F G H$.
$A B=5 \mathrm{~cm}$.
$B C=7 \mathrm{~cm}$.
$A E=3 \mathrm{~cm}$.
(a) Calculate the length of $A G$.

Give your answer correct to 3 significant figures.
(b) Calculate the size of the angle between $A G$ and the face $A B C D$.

Give your answer correct to 1 decimal place.
$\qquad$
16. In a factory, chemical reactions are carried out in spherical containers.

The time, $T$ minutes, the chemical reaction takes is directly proportional to the square of the radius, $R$ cm , of the spherical container.

When $R=120, T=32$
Find the value of $T$ when $R=150$

$$
T=.
$$

17. X and Y are two geometrically similar solid shapes.

The total surface area of shape $X$ is $450 \mathrm{~cm}^{2}$. The total surface area of shape $Y$ is $800 \mathrm{~cm}^{2}$.

The volume of shape X is $1350 \mathrm{~cm}^{3}$.
Calculate the volume of shape Y .
18. The time period, $T$ seconds, of a pendulum is calculated using the formula

$$
T=6.283 \times \sqrt{\frac{L}{g}}
$$

where $L$ metres is the length of the pendulum and $g \mathrm{~m} / \mathrm{s}^{2}$ is the acceleration due to gravity.
$L=1.36$ correct to 2 decimal places.
$g=9.8$ correct to 1 decimal place.
Find the difference between the lower bound of $T$ and the upper bound of $T$.
19. Simplify

$$
\frac{4 x^{2}-9}{2 x^{2}-5 x+3}
$$

20. In a game of chess, you can win, draw or lose.

Gary plays two games of chess against Mijan.
The probability that Gary will win any game against Mijan is 0.55
The probability that Gary will win draw game against Mijan is 0.3
(a) Work out the probability that Gary will win exactly one of the two games against Mijan.

In a game of chess, you score
1 point for a win
$\frac{1}{2}$ point for a draw,
0 points for a loss
(b) Work out the probability that after two games, Gary's total score will be the same as Mijan's total score.
21. (a) On the grid opposite, draw the graphs of

$$
x^{2}+y^{2}=100
$$

and

$$
\begin{equation*}
2 y=3 x-4 \tag{3}
\end{equation*}
$$

(b) Use the graphs to estimate the solutions of the simultaneous equations

$$
x^{2}+y^{2}=100
$$

and

$$
2 y=3 x-4
$$

For all the values of $x$

$$
x^{2}+6 x=(x+3)^{2}-q
$$

(c) Find the value of $q$.

$$
q=.
$$

$\qquad$

One pair of integer values which satisfy the equation

$$
x^{2}+y^{2}=100
$$

is $x=6$ and $y=8$
(d) Find one pair of integer values which satisfy

$$
x^{2}+6 x+y^{2}-4 y-87=0
$$

$$
\begin{equation*}
x=\ldots . . . . . . . . . . ., y=. \tag{3}
\end{equation*}
$$


(Total 10 marks)
22. In triangle $P Q R$, $P Q=10 \mathrm{~cm}$.
$Q R=12 \mathrm{~cm}$.
Angle $P Q R=45^{\circ}$.
(a) Calculate the area of triangle $P Q R$.

Give your answer correct to 3 significant figures.


The diagram shows triangle $A B C$ and triangle $A C D$.
$B C D$ is a straight line.
The perpendicular distance from $A$ to the line $B C D$ is $h \mathrm{~cm}$.
(b) Explain why $\frac{\text { area of triangle } A B C}{\text { area of triangle } A C D}=\frac{B C}{C D}$


The diagram shows triangle $X Y Z$.
$W$ is the point on $Y Z$ such that angle $Y X W=$ angle $W X Z$.
(c) Using expressions for the area of triangle $Y X W$ and the area of triangle $W X Z$, or otherwise, show that

$$
\frac{X Y}{X Z}=\frac{Y W}{W Z}
$$

