

Paper References(s)

## 5505/05 Edexcel GCSE Mathematics A – 1387 Paper 5 (Non-Calculator)

# **Higher Tier**

# Friday 5 November 2004 – Morning Time: 2 hours

#### Materials required for examination

Ruler graduated in centimetres and millimetres, protractor, compasses, pen, HB pencil, eraser. Tracing paper may be used. **Items included with question papers** Nil

#### **Instructions to Candidates**

In the boxes above, write your centre number, candidate number, your surname, initials and signature. Check that you have the correct question paper.

Answer ALL the questions in the spaces provided in this question paper.

You must NOT write on the formulae page or any blank pages. Anything you write on these pages will gain NO credit.

If you need more space to complete your answer to any question, use additional answer sheets.

#### **Information for Candidates**

The total mark for this paper is 100. This paper has 23 questions. There is one blank page. The marks for individual questions and parts of questions are shown in round brackets: e.g. (2). Calculators must not be used.

#### Advice to Candidates

Show all stages in any calculations. Work steadily through the paper. Do not spend too long on one question. If you cannot answer a question, leave it and attempt the next one. Return at the end to those you have left out.

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#### Answer ALL TWENTY THREE questions.

#### Write your answers in the spaces provided.

#### You must write down all stages in your working.

#### You must NOT use a calculator.

1. Rosa prepares the ingredients for pizzas.

She uses cheese, topping and dough in the ratio 2:3:5Rose uses 70 grams of dough.

Work out the number of grams of cheese and the number of grams of topping Rosa uses.

Cheese.....g

Topping .....g (Total 3 marks)

2. Work out

 $12\frac{1}{2} \div \frac{5}{8}$ 

(Total 3 marks)

.....

**3.** (a) Expand the brackets  $p(q-p^2)$ 

(b) Expand and simplify 5(3p+2) - 2(5p-3)

(2) (Total 3 marks)

.....

.....

(2)

**4.** (*a*) (i) Write 40 000 000 in standard form.

(ii) Write  $3 \times 10^{-5}$  as an ordinary number

(*b*) Work out the value of

 $3 \times 10^{-5} \times 40 \ 000 \ 000$ 

Give your answer in standard form.

(2) (Total 4 marks)

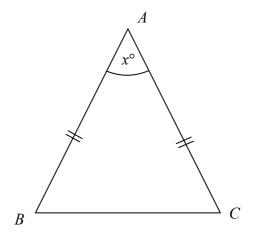


Diagram **NOT** accurately drawn

AB = ACAngle  $A = x^{\circ}$ 

(a) Find an expression, in terms of x, for the size of angle B.

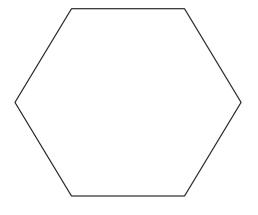
(b) Solve the simultaneous equations

$$3p + q = 11$$
$$p + q = 3$$

.....

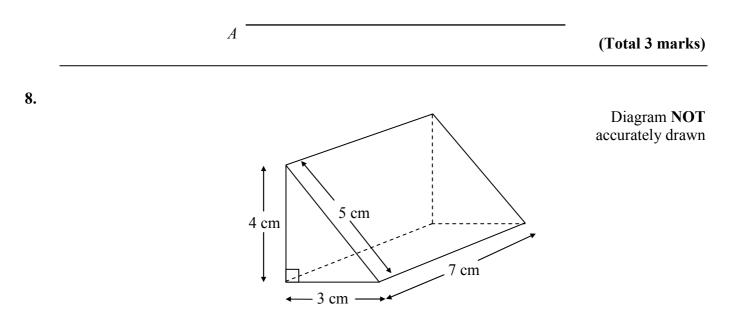
(2)

Diagram **NOT** accurately drawn



Calculate the size of the exterior angle of a regular hexagon.

.....° (2) (Total 2 marks) 7. Use ruler and compasses to **construct** an angle of  $45^{\circ}$  at *A*. You must show **all** construction lines.



Calculate the volume of the triangular prism.

(i) 
$$\frac{x^6}{x^2}$$

(ii) 
$$(y^4)^3$$

(2)

.....

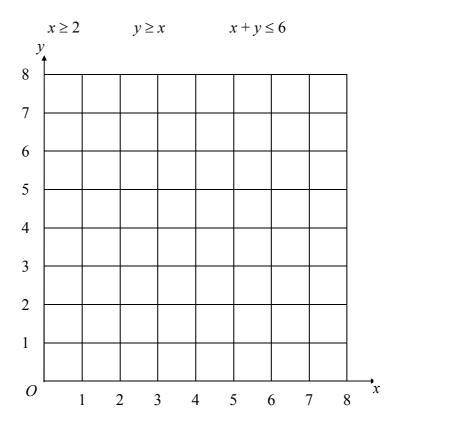
(b) Expand and simplify (t+4)(t-2)

(2)

(c) Write down the integer values of x that satisfy the inequality

 $-2 \le x < 4$ 

(d) Find the value of (i)  $36^{-\frac{1}{2}}$ (ii)  $27^{\frac{2}{3}}$ (iii)  $27^{\frac{2}{3}}$ (iv)  $(1000)^{\frac{1}{3}}$  10. (a) On the grid below, draw straight lines and use shading to show the region **R** that satisfies the inequalities



The point *P* with coordinates (x, y) lies inside the region **R**. *x* and *y* are **integers**.

(b) Write down the coordinates of **all** points of **R** whose coordinates are both integers.

(2) (Total 5 marks)

11. Make *u* the subject of the formula

$$D = ut + kt^2$$

*u* = .....(Total 2 marks)

(3)

Age (A) in years	Frequency
$15 < A \le 25$	44
$25 < A \le 35$	56
35 < <i>A</i> ≤ 45	34
45 < <i>A</i> ≤ 55	19
55 < <i>A</i> ≤ 65	7

12. The table gives information about the ages of 160 employees of an IT company.

(*a*) Complete the cumulative frequency table.

Age (A) in years	Cumulative Frequency
$15 < A \le 25$	
$15 < A \le 35$	
$15 < A \le 45$	
$15 < A \le 55$	
$15 < A \le 65$	

(1)

(b) On the grid opposite, draw a cumulative frequency graph for your table.

(2)

- (c) Use your graph to find an estimate for
  - (i) the median age of the employees,

..... years

(i) the interquartile range of the ages of the employees.

..... years (3)

Another IT company has 80 employees.

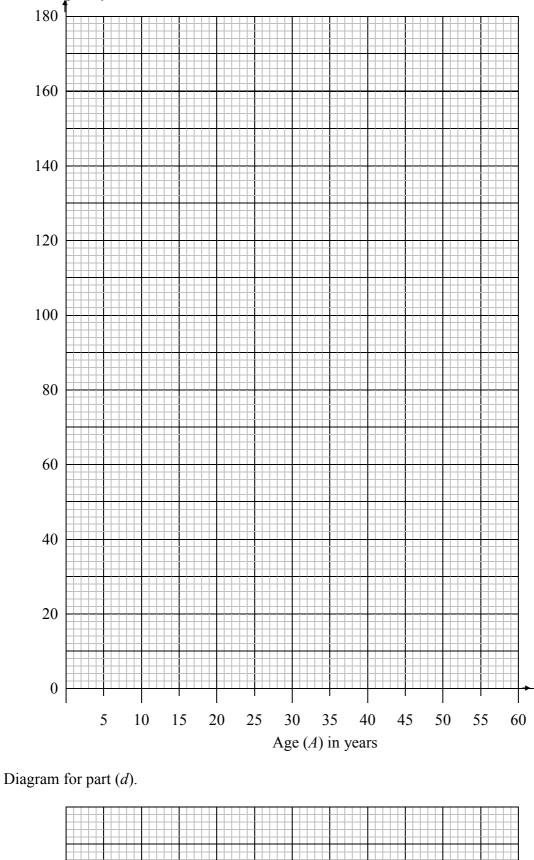
The age of the youngest employee is 24 years. The age of the oldest employee is 54 years.

The median age is 38 years. The lower quartile is 30 years. The lower quartile is 44 years.

(d) On the grid opposite, draw a box plot to show information about the ages of the employees.

(2) (Total 8 marks)

## Cumulative frequency



Turn over

Age (A) in years

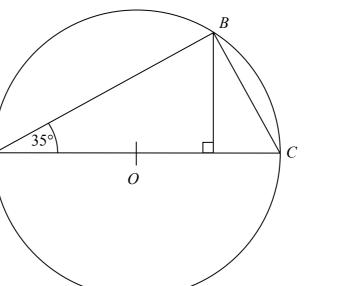


Diagram **NOT** accurately drawn

The diagram shows a circle, centre O.

A

AC is a diameter. Angle  $BAC = 35^{\circ}$ . D is the point on AC such that angle BDA is a right angle.

(*a*) Work out the size of angle *BCA*. Give reasons for your answer.

.....° (2)

(b) Calculate the size of angle DBC.

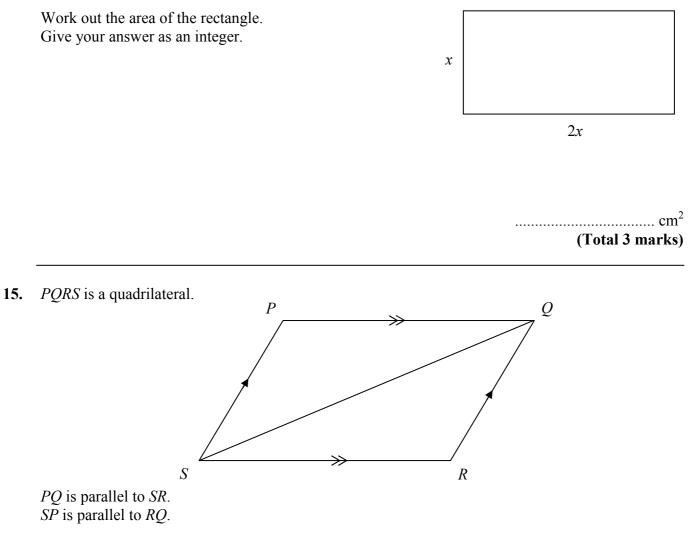
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(c) Calculate the size of angle *BOA*.

······ (2)

(Total 5 marks)

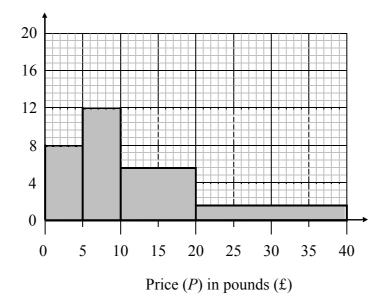
14. The length of a rectangle is twice the width of the rectangle. The length of a diagonal of the rectangle is 25 cm.



(a) Prove that triangle PQS is congruent to triangle RSQ.

(b) In quadrilateral *PQRS*, angle *SPQ* is obtuse. Explain why *PQRS* cannot be a cyclic quadrilateral. (3)

**16.** This histogram gives information about the books sold in a bookshop one Saturday.



(*a*) Use the histogram to complete the table.

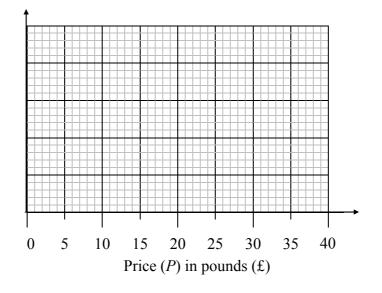
Price (P) in pounds (£)	Frequency
$0 < P \le 5$	
$5 < P \le 10$	
$10 < P \le 20$	
$20 < P \le 40$	

(2)

The frequency table below gives information about the books sold in a second bookshop on the same Saturday.

Price (P) in pounds (£)	Frequency
$0 < P \le 5$	80
$5 < P \le 10$	20
$10 < P \le 20$	24
$20 < P \le 40$	96

(b) On the grid below, draw a histogram to represent the information about the books sold in the second bookshop.

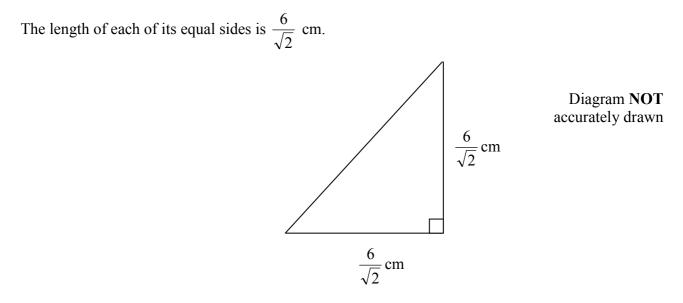


(3) (Total 5 marks)

17. (a)Express  $\frac{6}{\sqrt{2}}$  in the form  $a\sqrt{b}$ , where a and b are positive integers.

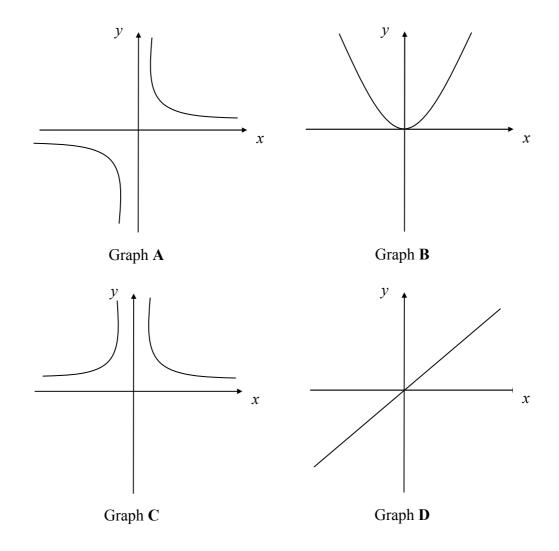
(2)

The diagram shows a right-angled isosceles triangle.



(b) Find the area of the triangle. Give your answer as an integer.

> ..... cm<sup>2</sup> (2) (Total 4 marks)



The graphs of y against x represent four different types of proportionality.

18.

Write down the letter of the graph which represents the type of proportionality.

Type of proportionality	Graph letter
<i>y</i> is directly proportional to <i>x</i>	
y is inversely proportional to $x$	
y is proportional to the square of $x$	
<i>y</i> is inversely proportional to the square of <i>x</i>	

### (Total 2 marks)

19. (a) Write down an expression, in terms of n, for the nth multiple of 5.

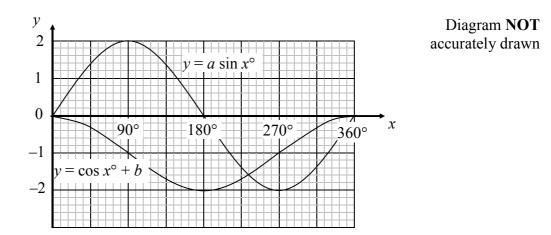
.....(1)

(b) Hence or otherwise

(i) prove that the sum of two consecutive multiples of 5 is always an odd number,

(ii) prove that the product of two consecutive multiples of 5 is always an even number.

(5) (Total 6 marks)



The diagram shows part of two graphs.

The equation of one graph is	$y = a \sin x^{\circ}$
The equation of the other graph is	$y = \cos x^\circ + b$

*a* = .....

*b* = .....(2)

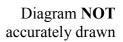
(b) Use the graphs to find the values of x in the range  $0 \le x \le 720^\circ$  when  $a \sin x^\circ = \cos x^\circ + b$ .

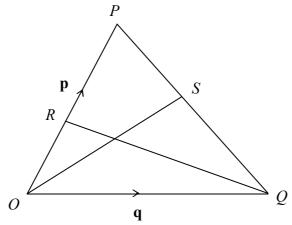
*x* = .....(2)

(c) Use the graphs to find the value of  $a \sin x^\circ - (\cos x^\circ + b)$  when  $x = 450^\circ$ .

(2) (Total 6 marks)

Turn over





*OPQ* is a triangle. *R* is the midpoint of *OP*. *S* is the midpoint of *PQ*.  $\overrightarrow{OP} = \mathbf{p}$  and  $\overrightarrow{OQ} = \mathbf{q}$ 

(i) Find  $\overrightarrow{OS}$  in terms of **p** and **q**.

(ii) Show that *RS* is parallel to *OQ*.

21.

 $\overrightarrow{OS}$  = .....

(Total 5 marks)

22. Solve 
$$\frac{2}{x+1} + \frac{3}{x-1} = \frac{5}{x^2-1}$$

x = .....(Total 4 marks)

23. The diagram shows a sector of a circle with a radius of x cm and centre O. PQ is an arc of the circle. Angle  $POQ = 120^{\circ}$ .

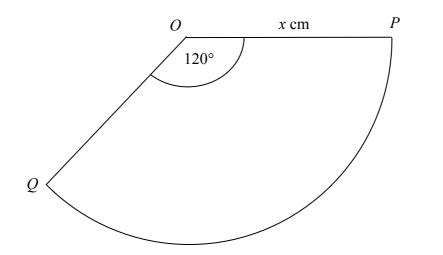


Diagram **NOT** accurately drawn

- (a) Write down an expression in terms of  $\pi$  and x for
  - (i) the area of this sector,
  - (ii) the arc length of this sector

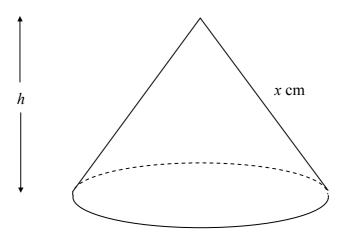
.....

.....

(2)

The sector is the net of the curved surface of this cone.

Arc PQ forms the circumference of the circle that makes the base of the cone.



The curved surface area of the cone is  $A \text{ cm}^2$ . The volume of the cone is  $V \text{ cm}^3$ . The height of the cone is h cm.

Given that V = 3A,

(*b*) find the value of *h*.

(3)

(Total 5 marks)

#### **TOTAL FOR PAPER: 100 MARKS**