| Centre <br> No. |  |  |  |  |  | Paper Reference |  |  |  |  | Initial(s) |  |  |  |  |
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| Candidate <br> No. |  |  |  |  |  |  | $\mathbf{5}$ | $\mathbf{5}$ | $\mathbf{0}$ | $\mathbf{6}$ | $\mathbf{0}$ | $\mathbf{0}$ |  | Signature |  |

Paper Reference(s)

Examiner's use only


Team Leader's use only
$\square$

Paper 6 (Calculator) Higher Tier
Tuesday 15 June 2004 - Morning


Time: 2 hours

Materials required for examination Ruler graduated in centimetres and Items included with question papers millimetres, protractor, compasses, pen, HB pencil, eraser, calculator. Tracing paper may be used.

## Instructions to Candidates

In the boxes above, write your centre number, candidate number, your surname, initials and signature.
You must NOT write on the formulae page or any blank pages. Anything you write on these pages will gain NO credit.
If you need more space to complete your answer to any question, use additional answer sheets.

## Information for Candidates

The total mark for this paper is 100 . This paper has 22 questions.
The marks for the various parts of questions are shown in round brackets: e.g. (2).
Calculators may be used.
If your calculator does not have a $\pi$ button, take the value of $\pi$ to be 3.142 unless the question instructs otherwise.

## Advice to Candidates

Show all stages in any calculations.
Work steadily through the paper. Do not spend too long on one question.
If you cannot answer a question, leave it and attempt the next one.
Return at the end to those you have left out.

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## GCSE Mathematics 1387/8

Higher Tier Formulae

## You must not write on this page.

Anything you write on this page will gain NO credit.

Volume of a prism $=$ area of cross section $\times$ length


Volume of sphere $=\frac{4}{3} \pi r^{3}$
Surface area of sphere $=4 \pi r^{2}$


In any triangle ABC


Sine Rule $\frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C}$
Cosine Rule $a^{2}=b^{2}+c^{2}-2 b c \cos A$

Area of triangle $=\frac{1}{2} a b \sin C$

Volume of cone $=\frac{1}{3} \pi r^{2} h$
Curved surface area of cone $=\pi r l$


The Quadratic Equation
The solutions of $a x^{2}+b x+c=0$
where $a \neq 0$, are given by

$$
x=\frac{\left.-b \pm \sqrt{\left(b^{2}-4 a c\right.}\right)}{2 a}
$$

## Answer ALL TWENTY TWO questions.

Write your answers in the spaces provided.
You must write down all stages in your working.

1. The manager of a school canteen has made some changes. She wants to find out what students think of these changes.

She uses this question on a questionnaire.
"How much money do you normally spend in the canteen?"


Design a better question for the canteen manager to use.
You should include some response boxes.
2. This is a map of part of Northern England.


Scale: 1 cm represents 10 km

A radio station in Manchester transmits programmes.
Its programmes can be received anywhere within a distance of 30 km .
On the diagram, shade the region in which the programmes can be received.
3. The table shows the number of computer games sold in a supermarket each month from January to June.

| Jan | Feb | Mar | Apr | May | Jun |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 147 | 161 | 238 | 135 | 167 | 250 |

(a) Work out the three month moving averages for this information.
$\qquad$
$\qquad$
$\qquad$
$\qquad$

In a sale, a supermarket took $20 \%$ off its normal prices.
On Fun Friday, it took $30 \%$ off its sale prices.
Fred says, "That means there was $50 \%$ off the normal prices".
(b) Fred is wrong. Explain why.

## (2)


4. The equation

$$
x^{3}-2 x=67
$$

has a solution between 4 and 5
Use a trial and improvement method to find this solution.
Give your answer correct to one decimal place.
You must show ALL your working.

$$
x=
$$

$\qquad$
5. A nanosecond is 0.000000001 second.
(a) Write the number 0.000000001 in standard form.
$\qquad$

A computer does a calculation in 5 nanoseconds.
(b) How many of these calculations can the computer do in 1 second? Give your answer in standard form.
6. Use your calculator to work out the value of $\frac{6.27 \times 4.52}{4.81+9.63}$
(a) Write down all the figures on your calculator display.
(b) Write your answer to part (a) to an appropriate degree of accuracy.
7. Here are some patterns made from dots.


Write down a formula for the number of dots, $d$, in terms of the Pattern number, $n$.
8.


Diagram NOT accurately drawn

An ice hockey puck is in the shape of a cylinder with a radius of 3.8 cm , and a thickness of 2.5 cm .

It is made out of rubber with a density of 1.5 grams per $\mathrm{cm}^{3}$.

Work out the mass of the ice hockey puck.
Give your answer correct to 3 significant figures.

9.


Diagram NOT accurately drawn
$D E=6 \mathrm{~m}$.
$E G=10 \mathrm{~m}$.
$F G=8 \mathrm{~m}$.
Angle $D E G=90^{\circ}$. Angle $E F G=90^{\circ}$.
(a) Calculate the length of $D G$.

Give your answer correct to 3 significant figures.
(b) Calculate the size of the angle marked $x^{\circ}$.

Give your answer correct to one decimal place.
10. Solve the simultaneous equations

$$
\begin{gathered}
6 x-2 y=33 \\
4 x+3 y=9
\end{gathered}
$$

$$
x=\text {. }
$$

$\qquad$

$$
y=.
$$

$\qquad$
11.


Pictures NOT accurately drawn

A 20 Euro note is a rectangle 133 mm long and 72 mm wide.
A 500 Euro note is a rectangle 160 mm long and 82 mm wide.
Show that the two rectangles are not mathematically similar.
12. A company bought a van that had a value of $£ 12000$ Each year the value of the van depreciates by $25 \%$.
(a) Work out the value of the van at the end of three years.
$\qquad$

The company bought a new truck.
Each year the value of the truck depreciates by $20 \%$.
The value of the new truck can be multiplied by a single number to find its value at the end of four years.
(b) Find this single number as a decimal.
13. A cone has a volume of $10 \mathrm{~m}^{3}$.

The vertical height of the cone is 1.5 m .
Calculate the radius of the base of the cone.
Give your answer correct to 3 significant figures.
14. Amy has 10 CDs in a CD holder.

Amy's favourite group is Edex.
She has 6 Edex CDs in the CD holder.
Amy takes one of these 10 CDs at random.
She writes down whether or not it is an Edex CD. She puts the CD back in the holder.
Amy again takes one of these 10 CDs at random.
(a) Complete the probability tree diagram.

First choice


Second choice


(2)
(b) Find the probability that Amy will pick two Edex CDs.

Amy had 30 CDs.
The mean playing time of these 30 CDs was 42 minutes.
Amy sold 5 of her CDs.
The mean playing time of the 25 CDs left was 42.8 minutes.
(c) Calculate the mean playing time of the 5 CDs that Amy sold.
15. The shutter speed, $S$, of a camera varies inversely as the square of the aperture setting, $f$.

When $f=8, S=125$
(a) Find a formula for $S$ in terms of $f$.
$\qquad$
(b) Hence, or otherwise, calculate the value of $S$ when $f=4$
$S=$ $\qquad$
(1)
16.

$A B=3.2 \mathrm{~cm}$.
$B C=8.4 \mathrm{~cm}$.
The area of triangle $A B C$ is $10 \mathrm{~cm}^{2}$.
Calculate the perimeter of triangle $A B C$.
Give your answer correct to three significant figures.
17.


Diagram NOT accurately drawn
$A T$ is a tangent at $T$ to a circle, centre $O$.
$O T=x \mathrm{~cm}, \quad A T=(x+5) \mathrm{cm}, \quad O A=(x+8) \mathrm{cm}$.
(a) Show that $x^{2}-6 x-39=0$
(b) Solve the equation $x^{2}-6 x-39=0$ to find the radius of the circle. Give your answer correct to 3 significant figures.
18.


Diagram NOT accurately drawn

The diagram represents a prism.
$A E F D$ is a rectangle.
$A B C D$ is a square.
$E B$ and $F C$ are perpendicular to plane $A B C D$.
$A B=60 \mathrm{~cm}$.
$A D=60 \mathrm{~cm}$.
Angle $A B E=90^{\circ}$.
Angle $B A E=30^{\circ}$.
Calculate the size of the angle that the line $D E$ makes with the plane $A B C D$.
Give your answer correct to 1 decimal place.
19. Bill said that the line $y=6$ cuts the curve $x^{2}+y^{2}=25$ at two points.
(a) By eliminating $y$ show that Bill is incorrect.
(b) By eliminating $y$, find the solutions to the simultaneous equations

$$
\begin{gathered}
x^{2}+y^{2}=25 \\
y=2 x-2
\end{gathered}
$$

$$
x=
$$

$\qquad$ $y=$ $\qquad$
$\qquad$ $y=$ $\qquad$
20. Martin won the 400 metre race in the school sports with a time of 1 minute.

The distance was correct to the nearest centimetre.
The time was correct to the nearest tenth of a second.
(a) Work out the upper bound and the lower bound of Martin's speed in $\mathrm{km} / \mathrm{h}$.

Give your answers correct to 5 significant figures.
Upper bound
km/h
Lower bound $\qquad$ km/h
(b) Write down an appropriate value for Martin's speed in $\mathrm{km} / \mathrm{h}$.

Explain your answer.
$\qquad$
$\qquad$

The table shows the number of people in each age group who watched the school sports.

| Age group | $0-16$ | $17-29$ | $30-44$ | $45-59$ | $60+$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Number of people | 177 | 111 | 86 | 82 | 21 |

Martin did a survey of these people.
He used a stratified sample of exactly 50 people according to age group.
(c) Work out the number of people from each age group that should have been in his sample of 50 .
Complete the table.

| Age group | $0-16$ | $17-29$ | $30-44$ | $45-59$ | $60+$ | Total |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Number of people <br> in sample |  |  |  |  |  |  |

21. (a) Solve $\frac{40-x}{3}=4+x$

$$
x=.
$$

(b) Simplify fully $\frac{4 x^{2}-6 x}{4 x^{2}-9}$
22.


The diagram shows a sketch of a curve.
The point $P(x, y)$ lies on the curve.
The locus of $P$ has the following property:
The distance of the point $P$ from the point $(0,2)$ is the same as the distance of the point $P$ from the $x$-axis.

Show that $\quad y=\frac{1}{4} x^{2}+1$

