

Paper 5506				
No	Working	Answer	Mark	Notes
1	(a) $V = \pi \times 4^2 \times 10$	$502 - 503 \text{ cm}^3$	2	M1 for $\pi \times 4^2 \times 10$ A1 502 – 503
	(b) $P^2 = 10^2 + 8^2$ $P = \sqrt{164}$	$\sqrt{164} < 13$	3	M1 for sight of correct right angled triangle M1 for $10^2 + 8^2$ A1 for conclusion based on a correct calculation Or 12.8 seen
2	(a)(i) $2 \times 30$	$2 \times 2 \times 3 \times 5$	4	M1 for systematic method, eg division, factor trees (at least one prime) A1 cao
	(ii) $2 \times 48$	$2^5 \times 3$		
	(b)	12	1	B1 cao
	(c) $2^5 \times 3 \times 5$	480	2	B2 cao B1 for $2^5 \times 3 \times 5$ or any correct common multiple

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3 (a)		$150 < C \leq 200$	2	M1 use of cum freq to find the cost of the 20 <sup>th</sup> or 20.5 <sup>th</sup> car OR $\frac{1}{2} \sum t^{\text{th}}$ or $\frac{1}{2} (\sum f + 1)^{\text{th}}$ car.
(b)		No, because the 21 <sup>st</sup> value is in the same interval	1	A1 eg 150 to 200, 150 – 200 B1 for 20.5 <sup>th</sup> or 21 <sup>st</sup> value in the same interval consistent with ‘a’ OR Refers to the median value being low in the interval (statement to be mathematically correct)
3 (c)	$80\% = 5200$ $\frac{5200}{80} \times 100$	6500	3	See additional sheet M1 for $(100 - 20)\% = 5200$ M1 for $\frac{5200}{"80"} \times 100$ A1 cao

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4	(a) $x^2(x + 1) = 230$  (b) 5 – 150 6 – 252 5.1 – 158.7 5.2 – 167.6  5.3 – 177.0  5.4 – 186.6 5.5 – 196.6 5.6 – 207.0 5.7 – 217.7 5.8 – 228.8 5.9 – 240.2 5.85 – 234.4	AG  5.8	2  4	M1 for $x \times x \times (x + 1)$ or $x \times x \times x + 1$ oe, $x^2(x + 1)$ , $x^2 \times x + 1$ A1 cao from $x \times x \times (x + 1)$ , no need to see 230  B2 for trial between 5.8 and 5.9 inclusive evaluated (B1 for trial between 5 and 6 inclusive evaluated)  B1 for different trial between 5.8 and 5.85 (not including 5.8) B1 dep on at least are previous B1 5.8, 5.81, 5.811
5	$\pi \times \left(\frac{15}{2}\right)^2 = 176.715$	88.4 cm <sup>2</sup>	3	M1 for $\pi \times \left(\frac{15}{2}\right)^2$ seen  A1 88.3 – 88.4 B1 for cm <sup>2</sup> (independent)

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6	(a) $5 = 0.5x + 1$	8	2	M1 for $5 = 0.5x + 1$ A1 cao
	(b)	$y = \frac{1}{2}x + c$	1	B1 for $y = \frac{1}{2}x + c, c \neq 1, oe$
	(c)	$x = 2y - 2$ OR $x = 2(y - 1)$	2	M1 for correctly multiplying both sides by 2 or correctly isolating $\frac{x}{2}$  A1 for $x = 2(y - 1), x = \frac{y-1}{0.5}, \frac{y-1}{\frac{1}{2}}$ oe  SC B1 for $x = 2y - 1$
7	$4x - 6y = 22$ $15x + 6y = 54$ $19x = 76$	$x = 4, y = -1$	4	M1 for coefficients of $x$ or $y$ the same followed by correct operation, allow one arithmetical error A1 cao M1 (dep) for correct sub for other variable A1 cao Trial and improvement 0 marks unless both correct values of $x$ and $y$ found
8	(a) $SF = \frac{10}{6}$ $\frac{10}{6} \times 4.8 = 8$	8	2	M1 for sight of $\frac{10}{6}$ or $\frac{6}{10}$ or 1.67 or better or $\frac{CD}{10} = \frac{4.8}{6}$ A1 cao
	(b) $\frac{10}{6} \times 4.5 - 4.5 = 3$	19.8	2	M1 for use of SF from "a" to find AC or BC or $\frac{BC}{4.5} = \frac{4}{6}$ and adding 4 sides A1 cao

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9	$\frac{6 \times 10^{15}}{3.2 \times 10^8}$ $1.875 \times 10^7$	$4.3 \times 10^3$	3	B3 for $4.3 \times 10^3$ to $4.34 \times 10^3$ (B2 for $1.875 \times 10^7$ oe or 4300 to 4340, final answer of $1.9 \times 10^7$ B1 for sight of $6 \times 10^{15}$ oe or $3.2 \times 10^8$ oe)
10	$8.5 \times \tan 38$ $= 8.5 \times 0.7813$ $\frac{8.5}{\sin(90 - 38)} = \frac{AB}{\sin 38}$ $AB = \frac{8.5 \times \sin 38}{\sin(90 - 38)}$ $= \frac{5.2331}{0.788} = 6.64$	6.64	3	M1 for correct use of trig, eg $\tan 38 = \frac{opp}{8.5}$ M1 for $8.5 \times \tan 38$ A1 6.64 – 6.641 OR M1 for correct substitution into the sine rule M1 (dep) for correct rearrangement for $AB =$ A1 6.64 – 6.641
11 (a)		No, as you would expect about 100. Yes, as it is possible to get 200 sixes with a fair dice	1	B1 for a consistent answer See additional sheet

No	Working	Answer	Mark	Notes
(b)	$\frac{1}{6}, \frac{5}{6} + \text{labels}$		3	B1 for $\frac{5}{6}$ on the red dice, <i>not six</i> branch B1 for a fully complete tree diagram with all branches labelled B1 for $\frac{1}{6}$ and $\frac{5}{6}$ on all remaining branches as appropriate
(c)(i)	$\left(\frac{1}{6}\right)^2$	$\frac{1}{36}$	2	M1 $\left(\frac{1}{6}\right)^2$ or $\frac{1}{6} \times \frac{1}{6}$ only or 0.28 A1 $\frac{1}{36}$ or 0.03 or better
(ii)	$1 - \left(\frac{5}{6}\right)^2$  OR $\frac{1}{6} \times \frac{5}{6} + \frac{5}{6} \times \frac{1}{6} + \frac{1}{6} \times \frac{1}{6}$	$\frac{11}{36}$	3	M2 for $1 - \left(\frac{5}{6}\right)^2$ or $1 - \frac{5}{6} \times \frac{5}{6}$ A1 cao  OR M1 for $\frac{1}{6} \times \frac{5}{6}$ oe M1 for 2 or 3 only of $\frac{1}{6} \times \frac{5}{6}, \frac{5}{6} \times \frac{1}{6}, "a"$  A1 for $\frac{11}{36}$ or 0.31 or better

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12 (a)	$\pi \times 30 \times \frac{7.5^2}{3} - \pi \times 10 \times \frac{2.5^2}{3} = 1767 - 65$	1700	3	M1 for either $\pi \times 30 \times \frac{7.5^2}{3}$ or $\pi \times 10 \times \frac{2.5^2}{3}$ M1 (dep) for difference A1 1700 – 1702 SC B1 Using d instead of r, 6800 – 6808
(b)	$\frac{S}{2\pi d} = \sqrt{h^2 + d^2}$ $\left(\frac{S}{2\pi d}\right)^2 = h^2 + d^2$	$h = \sqrt{\frac{S^2 - 4\pi^2 d^4}{4\pi^2 d^2}}$	3	M1 for correctly isolating $\sqrt{h^2 + d^2}$ or $h^2 + d^2$ or $h + d$ or $kh^2$ or $kh$ M1(indep) squaring both sides A1 $h = \sqrt{\frac{S^2 - 4\pi^2 d^4}{4\pi^2 d^2}}, \quad h = \frac{\sqrt{S^2 - 4\pi^2 d^4}}{2\pi d}$ $h = \sqrt{\left(\frac{S}{2\pi d}\right)^2 - d^2}$
12 (c)	$\left(\frac{30}{20}\right)^2 \times 450 \text{ or } 450 \div \left(\frac{20}{30}\right)^2$	1012.5	2	M1 for sight of correct SF <sup>2</sup> including 4:9 A1 1010 to 1013

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13 (a)	$\frac{2x(x+20)}{2} = 400$	As given	2	M1 $\frac{2x(x+20)}{2}$ or $\frac{2x \times x + 20}{2}$ or $2x(x+20) = 800$ A1 cao following correct working, no need for = 400 SC BI $2x \times x + \frac{1}{2} \times 2x(10 - \frac{x}{2}) \times 2$
13 (b)	$\frac{-20 \pm \sqrt{20^2 - 4 \times 1 \times (-400)}}{2}$ $= \frac{-20 \pm 44.721}{2}$	12.361	3	M1 for correct sub, up to signs, in the quad formula A1 for 44.7 or $\sqrt{2000}$ A1 for 12.3606 – 12.361, ignore negative solution T.I B3 for 12.361  OR Completing the square M1 for $(x+10)^2$ seen A1 for $-10 \pm \sqrt{500}$ A1 for 12.3606 – 12.361 ignore negative solution



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14	<p>(a) <math>0.5 \times 8 \times 15 \times \sin 70^\circ</math></p> <p>(b) <math>AB^2 = 8^2 + 15^2 - 2 \times 8 \times 15 \times \cos 70^\circ = 206.9</math></p> <p>EITHER  <math>0.5 \times AB \times CX = 56.38</math></p> <p>OR  <math>\frac{\sin B}{8} = \frac{\sin 70}{\sqrt{206.9}}</math>  <math>B = 31.5</math>  <math>15 \sin '31.5'</math></p>	<p>56.4</p> <p>7.84</p>	<p>2</p> <p>4</p>	<p>M1 for correct sub into area formula  A1 56.38 – 56.4</p> <p>M1 for correct sub into cos rule  A1 for 206.9 - 207 or 14.38 – 14.4</p> <p>EITHER  M1 for use of area rule to find CX  A1 7.83 – 7.84</p> <p>OR  M1 for correct use of sine rule to find sin B or sin A and then sight of <math>15 \sin B</math> or <math>8 \sin A</math>  A1 7.83 – 7.84</p>

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15	<p>(a) <math>4a^2 - 4a + 1 - (4b^2 - 4b + 1) =</math></p> $4(a^2 - b^2) - 4(a - b)$ $4(a - b)(a + b - 1)$ <p>OR</p> $((2a - 1) - (2b - 1))((2a - 1) + (2b - 1))$ $(2a - 2b)(2a + 2b - 2)$	AG	3	<p>Expansion Method</p> <p>M1 for a correct expansion of any one of the three terms</p> <p>M1(dep) on an attempt to expand all 3 terms and show LHS = RHS</p> <p>A1 fully correct algebra</p> <p>RHS exp is <math>4(a^2 + ab - a - ba - b^2 + b)</math></p> <p>OR Factorisation Method</p> <p>M1 for attempt to use difference of 2 squares on LHS</p> <p>M1 for one bracket correctly simplified</p> <p>A1 fully correct</p>
	<p>(b) Any 2 odd square numbers have the above form</p> <p>If <math>a</math> and <math>b</math> are both even or odd then <math>a - b</math> is even, so <math>4(a - b)</math> is a multiple of 8</p> <p>If one of <math>a, b</math> is odd, then <math>a + b - 1</math> is even, so <math>4(a + b - 1)</math> is a multiple of 8</p>		3	<p>B1 'any 2 square nos have the above form' (may be implied by sight of <math>(2a - 1)^2 - (2b - 1)^2</math> in part (b))</p> <p>B1 first reason</p> <p>B1 second reason</p> <p>SC B1 for <math>(2r + 1)^2 - (2r - 1)^2</math></p> <p>B1 for <math>8r</math></p>
16	<p>(a) <math>g_L = \frac{2 \times 4.495}{1.35^2 \times \sin 30.5}</math></p> $g_u = \frac{2 \times 4.505}{1.25^2 \times \sin 29.5}$	9.719	4	<p>B2 for any 4 of 4.505, 1.25, 29.5, 4.495, 1.35, 30.5 seen (B1 for any two or three seen)</p> <p>B1 for 11.710 – 11.7103</p> <p>B1 cao 9.719 – 9.71904</p>
	<p>(b) Round, until lower and upper bounds agree</p>	10	1	<p>B1 for 10 + reason “ they agree to this level of accuracy”</p>

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17	(a)(i) (ii) (iii)  (b) Divide to get $2y = 1$	$xy$ $y^2$ $\frac{x}{2}$ $q = -1$  $p = 6$	3    2	B1 cao B1 for $y^2$ or $y \times y$ B1 for $\frac{x}{2}$ or $0.5x$ or $2^{-1}x$ M1 for $2y = 1$ or $\frac{x}{2} = 32$ or $p + q = 5$ or $1 + p + 2q = 5$ A1 cao
18	(a) $x^2 - 2mx + m^2 - k$    (b)(i) Min value is $-m^2$  (ii) $x = m$	$k = m^2$    $-m^2$  $m$	2    3	M1 for correct exp of $(x - m)^2$ or correct completion of the square eg $\left(x - \frac{2m}{2}\right)^2 - \left(\frac{2m}{2}\right)^2$ A1 cao SC B1 for $k = -m^2$ M1 for recognition that min value occurs when $(x - m)^2 = 0$ (either (b)(i) or (b)(ii) correct implies this M1) A1 ft on 'k', "-k" gets M1 A0 A1 cao
19	$0.06 \times 0.05 = 0.003$	No	2	M1 for $0.06 \times 0.05$  A1 correct conclusion based on 0.003 or $0.06 \times 0.05$ stated as $\neq 0.0011$ OR M1 for statement that for the two events to be independent $P(\text{BL and CL}) = P(\text{BL}) \times P(\text{CL})$

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20		50 50 4	3	B1 50 or $\frac{100}{2}$ B1 for 50 or "a" B1 4 or $\frac{360}{90}$ oe